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# **SCOUR IN SUPERCRITICAL FLOW**

**Final Report**

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## SI UNIT CONVERSION FACTORS

The material contained in this report is presented in terms of English units. The following factors may be used to convert between measures used in this report and the International System of Units (SI):

1 foot = 0.3048 meter

1 meter = 3.2808 feet

1 foot per second (fps) = 0.3048 meters per second

1 meter per second = 3.2808 feet per second

1 cubic foot per second (cfs)

= 0.0283 cubic meters per second

1 cubic meter per second = 35.31 cubic feet per second

## SCOUR IN SUPERCRITICAL FLOW

### LIST OF SYMBOLS

- a exponent in power law approximation of function  
in Laursen sediment transport relation
- A coefficient in power law approximation of function  
in Laursen sediment transport relation
- $\alpha$  angle of attack for a pier ( $^{\circ}$ )
- b width of pier (ft) (unusual geometry can  
give difficulty in averaging to obtain  
a representative width)
- B width of rectangular channel between banks (ft)  
(If channel is not rectangular the width  
should be that of an equivalent rectangular  
channel; i.e., one which will carry the  
 $Q$  and  $Q_s$  at the same slope)
- c sediment load concentration in percent by weight
- C coefficient for shear factor  
(see Fig. 3 and Eq. (16), Page 16)
- d diameter of sediment particles (ft) (in this study  
a single size sediment is assumed)
- D diameter of circular pier (ft)
- $d_s$  depth of scour measured from the stream bed (ft)  
(other definitions of depth of scour  
can be appropriate for various problems)

LIST OF SYMBOLS (Continued)

F	Froude number of the flow, $V/\sqrt{gy}$
F <sub>C</sub>	threshold Froude number used in Eq. (2)
g	acceleration of gravity (fps <sup>2</sup> )
K	coefficient for hydraulic radius factor, R/y
K <sub>L</sub>	loss coefficient , $h_L = K_L(V_2^2/2g - V_1^2/2g)$
l	effective length of an abutment (ft), $l = Q_o/V_oY_o$ where $Q_o$ is the overbank flow obstructed by the embankment/abutment, and $V_o$ and $y_o$ are characteristic of the flow approaching the abutment scour hole
L	length of pier (ft)
n	resistance coefficient in Manning Equation
Q	water discharge (cfs)
Q <sub>C</sub>	water discharge within channel (ft)
Q <sub>O</sub>	water discharge on overbank(s) as appropriate
Q <sub>S</sub>	sediment load (tons per day)
Q <sub>t</sub>	total water discharge (cfs), the sum of $Q_c + Q_o$
Q <sub>w</sub>	water discharge approaching abutment scour hole in a width, $w = 2.75 d_s$ (cfs)
R	hydraulic radius (ft)
S	stream slope (ft/ft)
τ <sub>C</sub>	critical tractive force or boundary shear often assumed to be $4d$ (psf)
τ <sub>O</sub>	boundary shear at streambed for a wide channel (psf)

LIST OF SYMBOLS (Continued)

- $\tau'_0$  boundary shear at streambed due to particle shear  
evaluated as  $v^2 d^{1/3}/30 y^{1/3}$  (psf)
- $\theta$  inclination of embankment/abutment ( $^\circ$ )
- V velocity of flow (fps)
- w fall velocity of quartz sphere in large  
quiescent tank of water (fps)
- or
- width (approximately  $2.75 d_s$ ) of approach  
flow of  $Q_w$  associated with  
abutment scour hole (ft)

The only superscript is a prime (') used to  
differentiate particle shear from total boundary shear.

Several subscripts are used as follows:

- o for a reference velocity or depth of flow,  
or a reference boundary shear, or the  
appropriate overland flow
- 1 for the velocity, depth or boundary shear  
in a wide, approach reach
- 2 for the velocity, depth or boundary shear  
in the narrow, contracted reach
- c for a critical tractive force (boundary shear)  
or threshold Froude number

and a few others as defined in this listing.

## Final Report

### SCOUR IN SUPERCRITICAL FLOW

#### ABSTRACT

Scour in supercritical flow is one extreme aspect of the effect of velocity on scour. Analysis of the case of scour in a long contraction shows that if all other independent variables are kept constant, (1) some finite velocity is necessary to have any scour, (2) as the velocity is increased, the scour increases as long as there is no sediment movement in the wide, approach reach, and (3) as sediment movement in the approach increases with further increase in the velocity, the scour decreases a modest amount. The analysis does not indicate that there should necessarily be a change in behavior in supercritical flow --although the definition of scour needs to consider velocity head changes and energy losses. Rather than velocity, the variable of interest should be the ratio of the particle shear to the critical tractive force.

Adaptation of the long-contraction solution to the case of the pier or abutment indicates that the scour at a pier or abutment should display the same behavior: scour increasing with velocity for the clear-water condition and decreasing slightly for sediment-transporting flow. Experiments agree with the analysis for both geometries. No instability of flow

or other "strange" behavior was noted in the supercritical flow, possibly because of the simplicity of the geometries, or because the equipment could not achieve high enough Froude numbers.

#### BACKGROUND OF THE PROBLEM

One of the findings of the Iowa investigation of scour around bridge piers and abutments (1, 2, 3) was that if the flow was transporting sediment, the scour depth, as a first approximation, was a function of geometry only. The notion that velocity and sediment size have little effect of scour depth has been difficult, if not impossible, for many people to understand or accept. "Everyone" knows that bridges may fail in floods, although some speak of "liquefaction" rather than scour holes, and others believe that the stream bed lowers as much as the water surface rises. Those who are aware of scour holes around the piers and abutments are often more impressed by the velocity of the flood water than the depth of the flood water; therefore, they naturally attribute the scour which occurs to the increase in the velocity of flow.

Scour occurs because of an imbalance between the capacity of the flow to remove sediment from an area and the supply of sediment to that area by the flow (4). If the capacity to remove sediment exceeds the supply, there will be scour. If the supply exceeds the capacity, there will be deposition. The limit to the scour or deposition is a geometry

such that the capacity equals the supply. When there is sediment transport by the stream, it does not matter much what the rate of sediment transport is (and, therefore, what the velocity and sediment size are) just so long as there is a balance between the amount of material coming into the area in question and the amount going out of the area. In the laboratory, the depth and other geometry can be kept constant and the velocity of flow increased (or the sediment size changed). The rate of transport will change but the scour depth will not measurably change if the boundary shear is well above the critical tractive force. In a real river in flood, both depth and velocity of flow increase, making it difficult to sort out what is doing what to what. In addition, it is possible for the flow pattern of the river to change with stage during the course of the flood, and the pier geometry can change with the accumulation of debris.

When the flow is not transporting material as large as the bed material which must be removed in the scour process, the condition is essentially that of clear-water flow and the sediment supply to the area in question is zero. The limit of scour is then a boundary shear equal to the critical tractive force of the material which could be scoured. The boundary shear is certainly a function of the velocity of flow and the critical tractive force is certainly a function of the sediment size. Both then matter (as well as geometry) in the depth of clear-water scour. Indeed, they matter together in a parameter

which is the ratio of the reference particle boundary shear to the reference critical tractive force; thus, if both velocity and sediment size increase, but the parameter stays the same, the scour depth does not change.

The controversy over the effect of velocity -- and/or sediment size -- has persisted since the publications resulting from the Iowa experiments. Several of the discussions of the ASCE paper (3) cited clear-water scour studies in disagreeing with the conclusion that in sediment-transporting flow there was little effect of velocity and sediment size on scour. The closing discussion tried to make the distinction clear in a qualitative argument which led to a subsequent paper on the clear-water scour case (5). Years later the small effect of velocity and sediment size was investigated (6, 7, 8) and it was found that the scour depth decreased with an increase in velocity or the particle shear/critical tractive force ratio. Straub, of course, had found the effect years earlier (9, 10) when he presented the first analytical long-contraction scour solution.

Over the years a number of investigators have proposed scour-prediction formulae which include the velocity in some way. Typical of these are those presented in a FHWA Training and Design Manual prepared by several of the Colorado State University Group (11). Their expression for the scour at a rectangular pier aligned with the flow can be written as

$$\frac{d_s}{b} = 2.2 \left( \frac{y_o}{b} \right)^{0.35} F^{0.43} \quad (1)$$



where  $d_s$  is the depth of scour measured from the stream bed,

$V_0$  is the depth of the approach flow,

$y_0$  is the depth of the approach flow,

$b$  is the width of the pier, and

$F$  is the Froude number of the approach flow,  $V_0 / \sqrt{gy_0}$ .

Several comments serve to increase this prediction of the "equilibrium" scour depth, "...maximum scour depth at piers could be as large as 30 percent greater than equilibrium scour depth" and "... $y_0$  would normally be measured from some level closer to the tops of dunes. Scour depths on the other hand should be referenced nearer the trough of the dunes." Elsewhere it is implied that the fluctuations above the average or equilibrium is due to the dunes, and these comments would seem to correct twice for the same phenomenon. However, this is a matter of the absolute value of the predicted depth of scour, not the question of the effect of velocity on scour. For two identical piers in identical rivers (except for the velocity) if the one river is in the Midwest with a Froude number of 0.2 and the other river is in the Southwest with a Froude number of 1.0, Eq. (1) would predict twice the scour depth in the Southwest as in the Midwest -- e.g., 20 feet compared to 10 feet. In general, the depths of scour predicted by Eq. (1), especially if increased as suggested for conditions in the Southwest are so large that if the predictions were correct, very few bridges over alluvial streams should be still standing in Arizona -- or lands like it. It is of

some interest to note that the sediment size does not affect the depth of scour predicted by Eq. (1).

A FHWA-sponsored project performed by the Iowa Institute of Hydraulic Research (12) on scour at Froude numbers up to 1.2 and 1.5 suggested a similar relationship which included sediment size in a threshold Froude number. The envelope curve included both pier scour and bed-form scour and was for a circular pier (a rectangular pier would experience 10% more scour).

$$\frac{d_s}{D} = 2.0 \left(\frac{y_0}{D}\right)^{0.5} (F - F_c)^{0.25} \quad (2)$$

where  $d_s$  is the total depth of scour measured from the stream bed,

$D$  is the diameter of the circular pier,

$y_0$  is the depth of flow,

$F$  is the Froude number of the flow, and

$F_c$  is the threshold Froude number based on a threshold velocity obtained from the Shields diagram and the logarithmic velocity distribution.

(This term involves the sediment size.)

Even if the coefficient in Eq. (2) is increased because of the shape factor, it will usually predict less scour than Eq. (1), especially if the Eq. (1) suggestions for increasing the predicted scour are followed. Because Eq. (2) includes the combined effect of pier scour and bed-form scour, it should embody (approximately) the suggestions for predicting scour by

Eq. (1). In general, Eq. (2) will predict about 50 percent more scour at high Froude numbers than would be predicted by the relationships proposed in References 2 and 3.

There is no theoretical basis for Eq. (2). It is similar to Eq. (1) which has no theoretical basis either, the difference being in the coefficient, the exponents, and the inclusion of a critical term. Both equations can best be described as power curve fitting to limited experimental data with parameters obtained from dimensional analysis. As usual, dimensional analysis doesn't get one very far; dimensional analysis requires, first, that one knows what variables are important (and independent) and, second, that one knows what dimensionless combinations are meaningful.

Having a suspicion of what laboratory equipment was used in these Iowa experiments, there is a chance that the scour measured is not necessarily the scour associated with the flow characteristics measured.

In recent years, the State of Arizona experienced several large floods and a number of bridges were lost or damaged. As a consequence, the Arizona Department of Transportation (and some cities and counties) have been trying to identify possible vulnerable bridges and then taking some action in the way of remedial works to make them less vulnerable. It makes a difference if the predicted scour is ten, fifteen or twenty feet. Streams in Arizona are relatively steep -- one-half of one percent or more, rather than a foot per mile -- and the

Froude number of streams in flood can approach or even exceed unity. Therefore, the need for this research is obvious and readily apparent.

#### THE LONG-CONTRACTION SOLUTION

Straub in his original analytic solution (9, 10) showed that in the long contraction the depth ratio  $y_2/y_1$  decreased as the ratio of boundary shear to critical tractive force  $\tau_1/\tau_c$  increased from slightly greater than unity. (At a ratio of unity his solution broke down.) His full equation was derived using the DuBoys sediment-transport equation and the Manning equation and is

$$\frac{y_2}{y_1} = \left(\frac{B_1}{B_2}\right)^{3/7} \left\{ \frac{-\frac{\tau_c}{\tau_1} + \left[ \left(\frac{\tau_c}{\tau_1}\right)^2 + 4 \left(1 - \frac{\tau_c}{\tau_1}\right) \frac{B_1}{B_2} \right]^{1/2}}{2 \left(1 - \frac{\tau_c}{\tau_1}\right)} \right\}^{3/7} \quad (3)$$

where  $\tau_c$  is the critical tractive force and the subscripts 1 and 2 refer to the wide approach, and narrow, contracted reaches, respectively.

When  $\tau_1/\tau_c$  is large ( $\infty$ ), the full solution reduces to

$$\frac{y_2}{y_1} = \left(\frac{B_1}{B_2}\right)^{9/14} \quad (4)$$

wherein the velocity, sediment size, Froude number and shear ratio, all have no effect on the depth ratio.

In Straub's full solution there is about a 15-percent decrease in the depth ratio as the shear ratio increases from 1.01 to  $\infty$ ; 10 percent occurring as the shear ratio increases from 1.01 to 2, and 5 percent occurring as the shear ratio increases from 2 to  $\infty$ .

Note that Straub's solution is for the sediment-transporting flow case only, not the clear-water case, that the full solution suffers from the use of the total boundary shear instead of the particle boundary shear in the Duboys sediment-load equation and probably should use Straub's evaluation of critical tractive force, but that for a river in flood the reduced equation (Eq. 4) is sufficient because the critical tractive force should then be small compared to the boundary shear.

A more general solution of long-contraction scour can be performed which will illustrate more fully the effect of velocity on scour. Figure 1 is a definition sketch of a general long contraction in which the total flow  $Q_t$  is divided between a portion  $Q_c$  in the approach channel of width  $B_1$  and a portion  $Q_o$  on the overbank, or floodplain. (The division of  $Q_o$  into two equal parts is immaterial.) If there is some additional overbank flow outside of the contracted channel of width  $B_2$ , it can simply be ignored; it is not doing anything of importance in this problem.

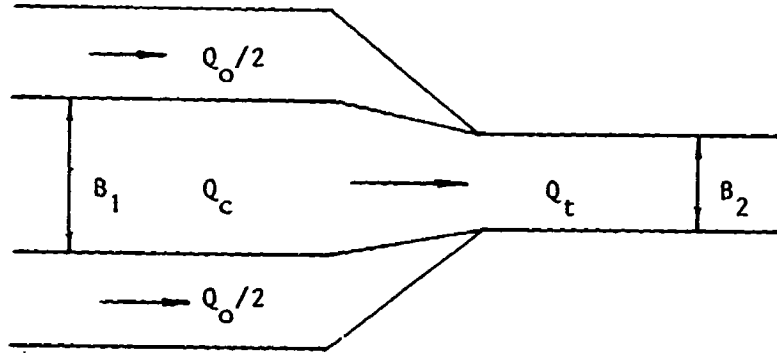


Figure 1. Definition Sketch of the General Long Contraction.

The solution of the clear-water case proceeds from the realization that if there is active scour in the long contraction, it will continue (slower and slower) until the particle boundary shear is equal to the critical tractive force. In the approach reach, the shear ratio will be less than unity. There will be some flow (some particle boundary shear in the approach) greater than zero when the shear ratio in the contraction is unity without any scour having taken place. If there is overbank flow in the approach, the width  $B_1$  should be increased so that the total flow will exist at the velocity and depth of the channel flow. The following evaluations and approximations are used:

$$\tau'_o = \frac{v^2 d^{1/3}}{30y^{1/3}} \quad (5)$$

where  $\tau'_o$  is the particle shear; i.e., the boundary shear for a wide channel with a "smooth" bed with a texture of the sand grains solved by the Manning equation and Strickler's  $n$ .

$$\tau_c = 4d \quad (6)$$

$$R = y \quad (7)$$

where the channel is wide so the hydraulic radius  $R$  equals the depth  $y$ .

With these, an expression is obtained for the depth ratio

$$\frac{y_2}{y_1} = \left(\frac{\tau'_1}{\tau_c}\right)^{3/7} \left(\frac{B_1}{B_2}\right)^{6/7} \quad (8)$$

The solution proceeds by writing

$$\tau'_2 = \frac{v_2^2 d^{1/3}}{30y_2^{1/3}} = \tau_c = 4d$$

$$\tau'_1 = \frac{v_1^2 d^{1/3}}{30y_1^{1/3}}$$

and

$$Q_1 = V_1 Y_1 B_1 = Q_2 = U_1 Y_2 B_2$$

and, then, equating

$$\frac{\tau_1'}{\tau_c} = \frac{\tau_1'}{\tau_2'}$$

This expression is shown graphically in Figure 2. Note that the depth ratio or the relative depth of scour (for many problems the depth of scour can be taken as  $y_2 - y_1$ ) is a function of the geometry  $B_1/B_2$  and the shear ratio which includes both velocity and sediment size (and depth). Other evaluations of the particle boundary shear and the critical tractive force could conceivably give a somewhat different expression or result in a slightly different answer in an application. The solution is of limited, but occasionally important, use in real river situations but, as will be seen, it can be adapted to the riprap problem. Its importance here is the light it sheds on the scour problem in general.

For the sediment-transporting flow case, more insight into the effect of velocity (or velocity-related parameters) on scour in the long contraction can be gained by a solution similar to Straub's but using several approximations of the Laursen sediment-transport relation (instead of the DuBoys equations), the Manning formula, and the other following statements, approximations and evaluations (6, 7, 8)



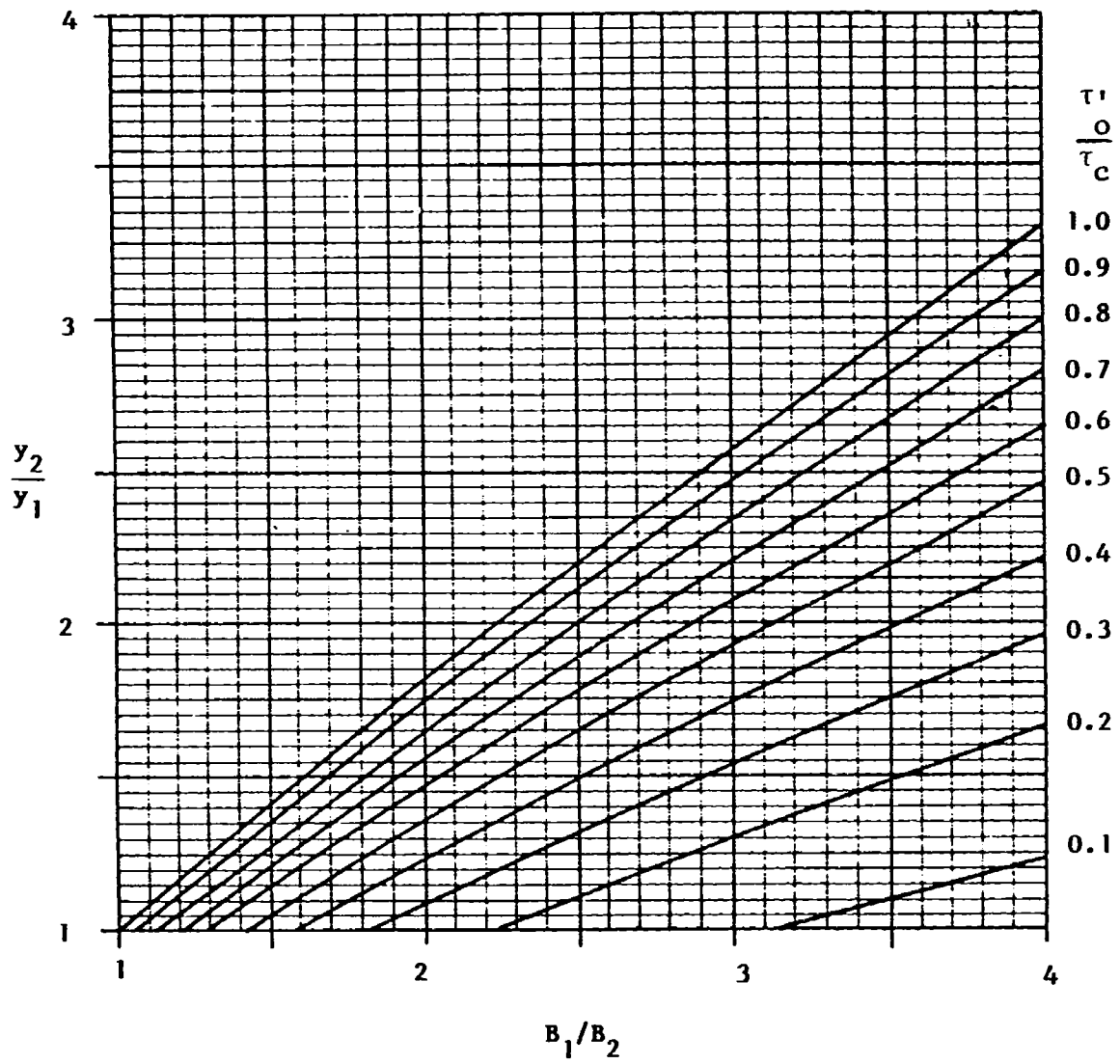


Figure 2. Clear-Water Scour in a Long Contraction.

$$Q_c = B_1 y_1 \frac{1.49}{n_1} R_1^{2/3} S_1^{1/2} \quad (9)$$

$$Q_t = B_2 y_2 \frac{1.49}{n_2} R_2^{2/3} S_2^{1/2} \quad (10)$$

$$Q_t = Q_c + Q_o \quad (11)$$

$$\bar{c}_1 Q_c = \bar{c}_2 Q_t \quad (12)$$

$$\bar{c}_1 = \left(\frac{d}{y_2}\right)^{7/6} \left(\frac{\tau_1}{\tau_c} - 1\right) A \left(\frac{\sqrt{\tau_1/\rho}}{w}\right)^a \quad (13)$$

$$\bar{c}_2 = \left(\frac{d}{y_2}\right)^{7/6} \left(\frac{\tau_2}{\tau_c} - 1\right) A \left(\frac{\sqrt{\tau_2/\rho}}{w}\right)^a \quad (14)$$

where  $Q_c$  is the between-banks discharge in the approach channel of width  $B_1$ , depth  $y_1$ , and slope  $S_1$ , and having a resistance coefficient  $n_1$ .

$Q_t$  is the total discharge confined within the long contraction of width  $B_2$ , depth  $y_2$ , and slope  $S_2$ , and having a resistance coefficient  $n_2$ .

$Q_o$  is the overbank (or floodplain) discharge which is here arbitrarily divided equally between the right and left sides.

The concentration of the sediment load  $\bar{c}$  is in percent by weight of a single size sediment of diameter  $d$ , critical tractive force  $\tau_c$ , and fall velocity  $w$ . A mixture, or

natural sediment, can be considered on a case-by-case basis, using the proper version of the Laursen total load relation but has not been generalized -- generalization may not be possible. The term  $\tau_o'$  is the "particle shear" as mentioned previously and  $\tau_o$  is the "total shear" ( $\gamma yS$ ). An alternate formulation of the shear velocity  $\sqrt{\tau_o/\rho}$  is  $\sqrt{gyS}$ . The subscripts 1 and 2 refer to the approach and contracted reaches, respectively, and the subscript o is dropped for simpler topography.

The function of  $\sqrt{\tau_o/\rho}/w$  in the Laursen sediment-transport relation is approximated by power functions over three ranges. One would expect that the approach and contracted reaches would be in the same range; further refinement would seldom be of interest. The intercept (A) values drop out of consideration and the exponent (a) values are

$$\sqrt{\tau_o/\rho}/w < 1/2 , \quad a = 1/4$$

$$\sqrt{\tau_o/\rho}/w = 1 \quad , \quad a = 1$$

$$\sqrt{\tau_o/\rho}/w > 2 \quad , \quad a = 9/4$$

The fall velocity  $w$  is that of a quartz sphere of diameter  $d$  falling in large quiescent container, just as was done in the development of the original relationship. A different, better

fall velocity for grains of sand and gravel would require revision of the function  $f(\sqrt{\tau_o/\rho} w)$ .

A rectangular cross section is assumed but not a very wide channel, so

$$R = Ky \tag{15}$$

The shear ratio term is written as

$$\frac{\tau_o'}{\tau_c} - 1 = C \frac{\tau_o'}{\tau_c} \tag{16}$$

This equation is shown graphically in Figure 3.

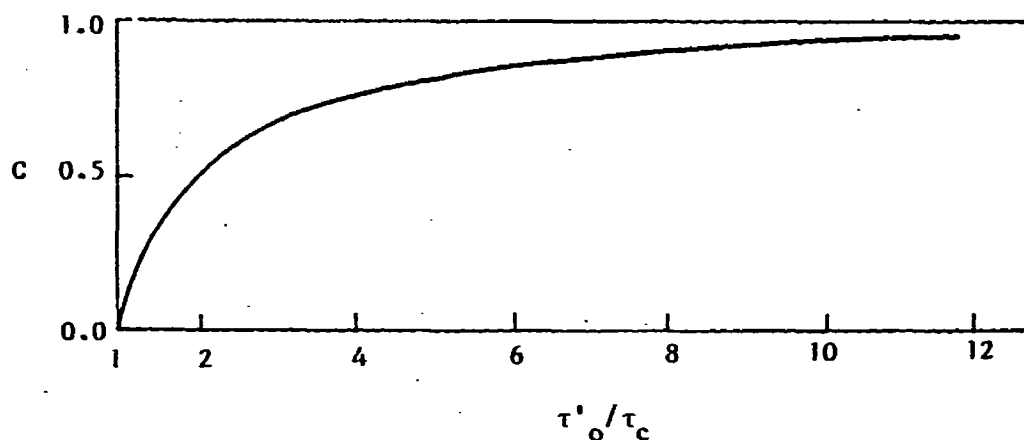


Figure 3. Critical-Tractive Force Term.

Equating the discharge and sediment load in the two reaches and manipulating algebraically to eliminate either the slopes or the depths, results in the following equations for the depth or slope ratios:

For bed load ( $\sqrt{\tau_o/\rho} / w < 1/2$ )

$$\frac{y_2}{y_1} = \left(\frac{Q_t}{Q_c}\right)^{0.86} \left(\frac{B_1}{B_2}\right)^{0.59} \left(\frac{n_2}{n_1}\right)^{0.07} \left(\frac{C_2}{C_1}\right)^{0.26} \left(\frac{K_1}{K_2}\right)^{0.01} \quad (17)$$

$$\frac{s_1}{s_2} = \left(\frac{Q_t}{Q_c}\right)^{0.86} \left(\frac{B_1}{B_2}\right)^{-0.02} \left(\frac{n_1}{n_2}\right)^{1.78} \left(\frac{C_2}{C_1}\right)^{0.88} \left(\frac{K_2}{K_1}\right)^{1.30} \quad (18)$$

For some suspended load ( $\sqrt{\tau_o/\rho} / w = 1$ )

$$\frac{y_2}{y_1} = \left(\frac{Q_t}{Q_c}\right)^{0.86} \left(\frac{B_1}{B_2}\right)^{0.64} \left(\frac{n_2}{n_1}\right)^{0.21} \left(\frac{C_2}{C_1}\right)^{0.21} \left(\frac{K_1}{K_2}\right)^{0.04} \quad (19)$$

$$\frac{s_1}{s_2} = \left(\frac{Q_t}{Q_c}\right)^{0.86} \left(\frac{B_1}{B_2}\right)^{0.14} \left(\frac{n_1}{n_2}\right)^{1.29} \left(\frac{C_2}{C_1}\right)^{0.71} \left(\frac{K_2}{K_1}\right)^{1.21} \quad (20)$$

For mostly suspended load ( $\sqrt{\tau_o/\rho} / w > 2$ )

$$\frac{y_2}{y_1} = \left(\frac{Q_t}{Q_c}\right)^{0.86} \left(\frac{B_1}{B_2}\right)^{0.69} \left(\frac{n_2}{n_1}\right)^{0.37} \left(\frac{C_2}{C_1}\right)^{0.16} \left(\frac{K_1}{K_2}\right)^{0.06} \quad (21)$$

$$\frac{s_1}{s_2} = \left(\frac{Q_t}{Q_c}\right)^{0.86} \left(\frac{B_1}{B_2}\right)^{0.31} \left(\frac{n_1}{n_2}\right)^{0.78} \left(\frac{C_2}{C_1}\right)^{0.54} \left(\frac{K_2}{K_1}\right)^{1.13} \quad (22)$$

The depth ratio for these three modes of movement are shown graphically in Figures 4, 5 and 6 as a function of width ratio and shear factor.

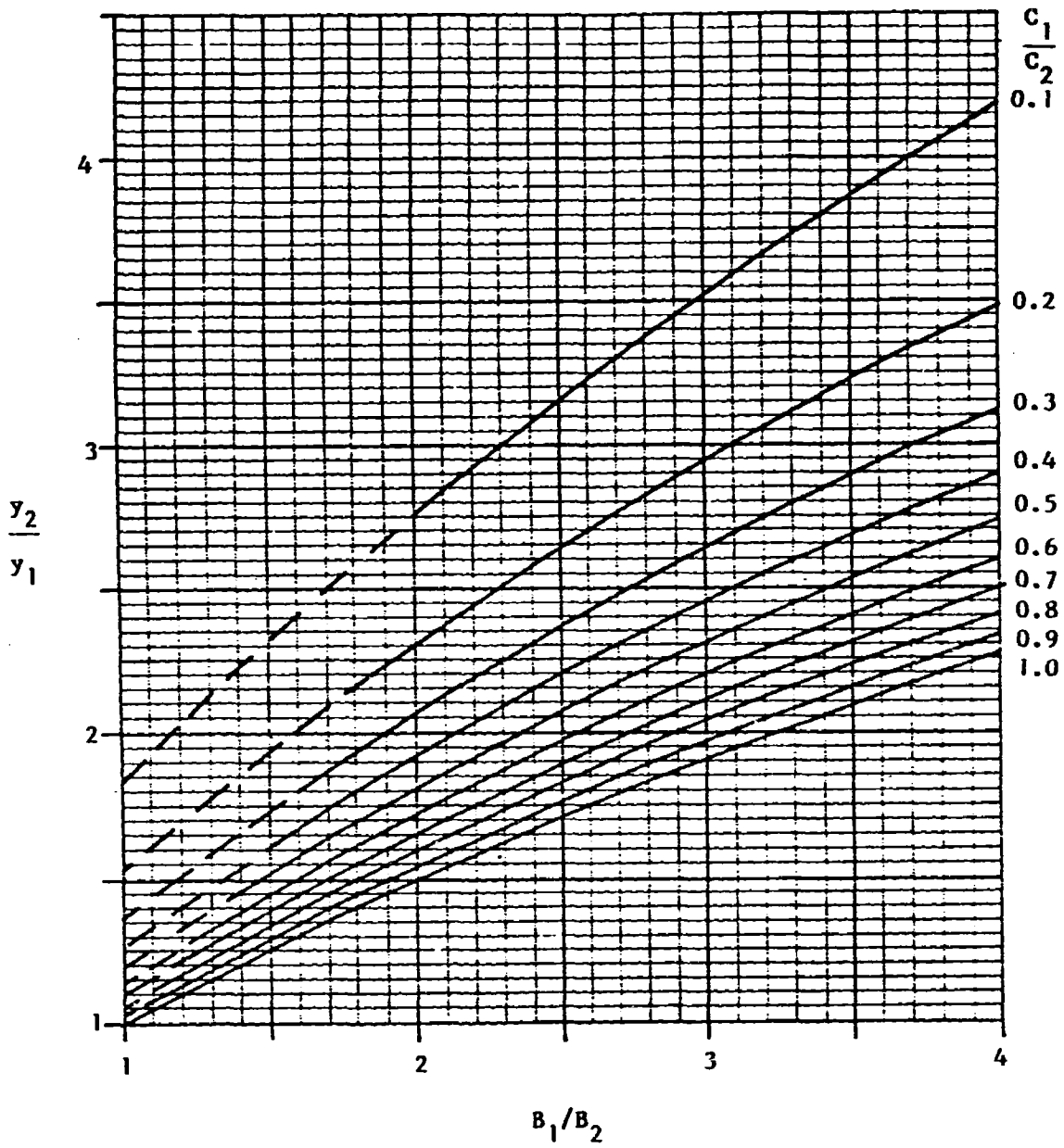


Figure 4. Depth Ratio vs Width Ratio and Shear Factor for Bed Load in a Long Contraction.

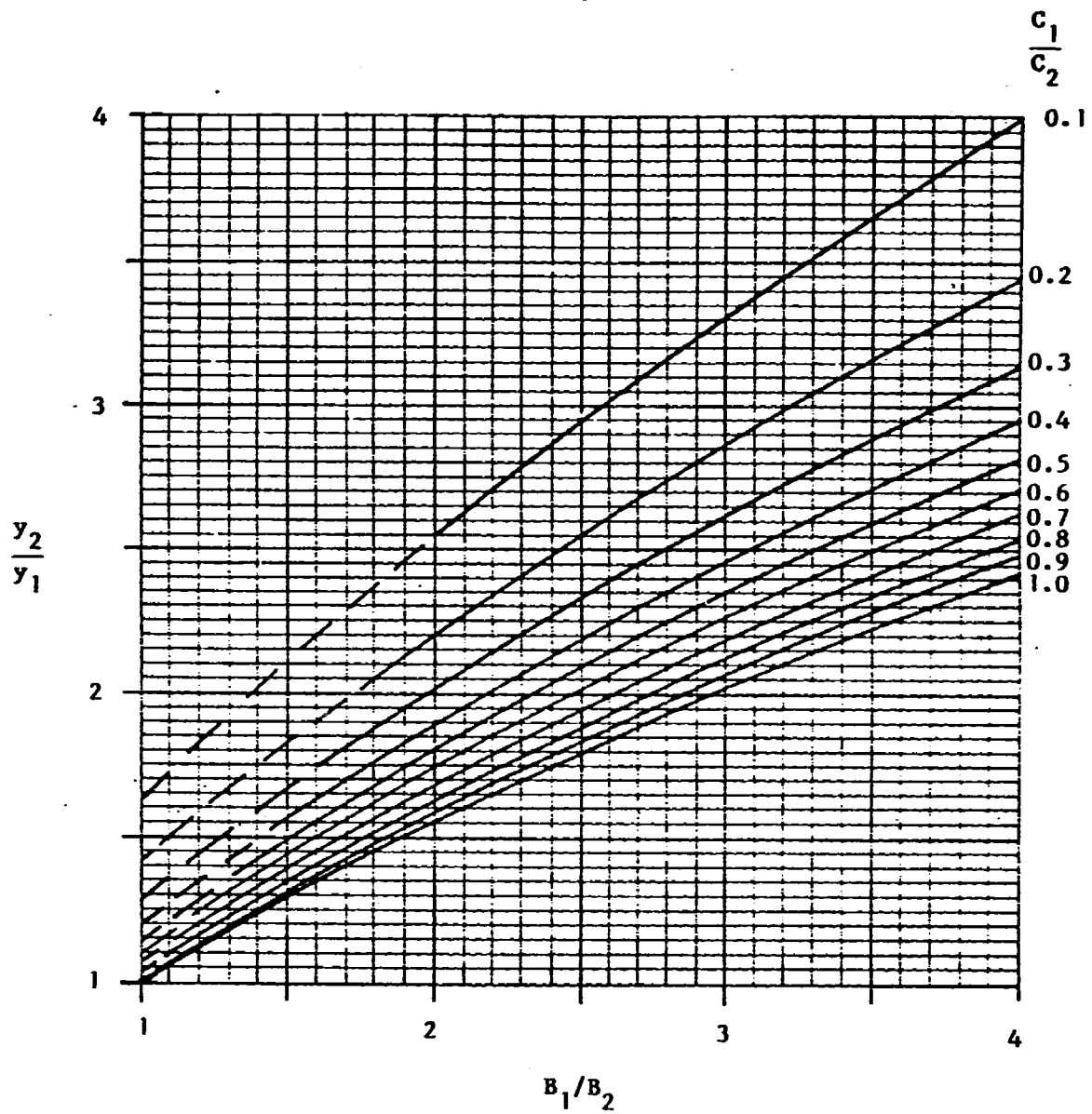


Figure 5. Depth Ratio vs Width Ratio and Shear Factor for Some Suspended Load in a Long Contraction.

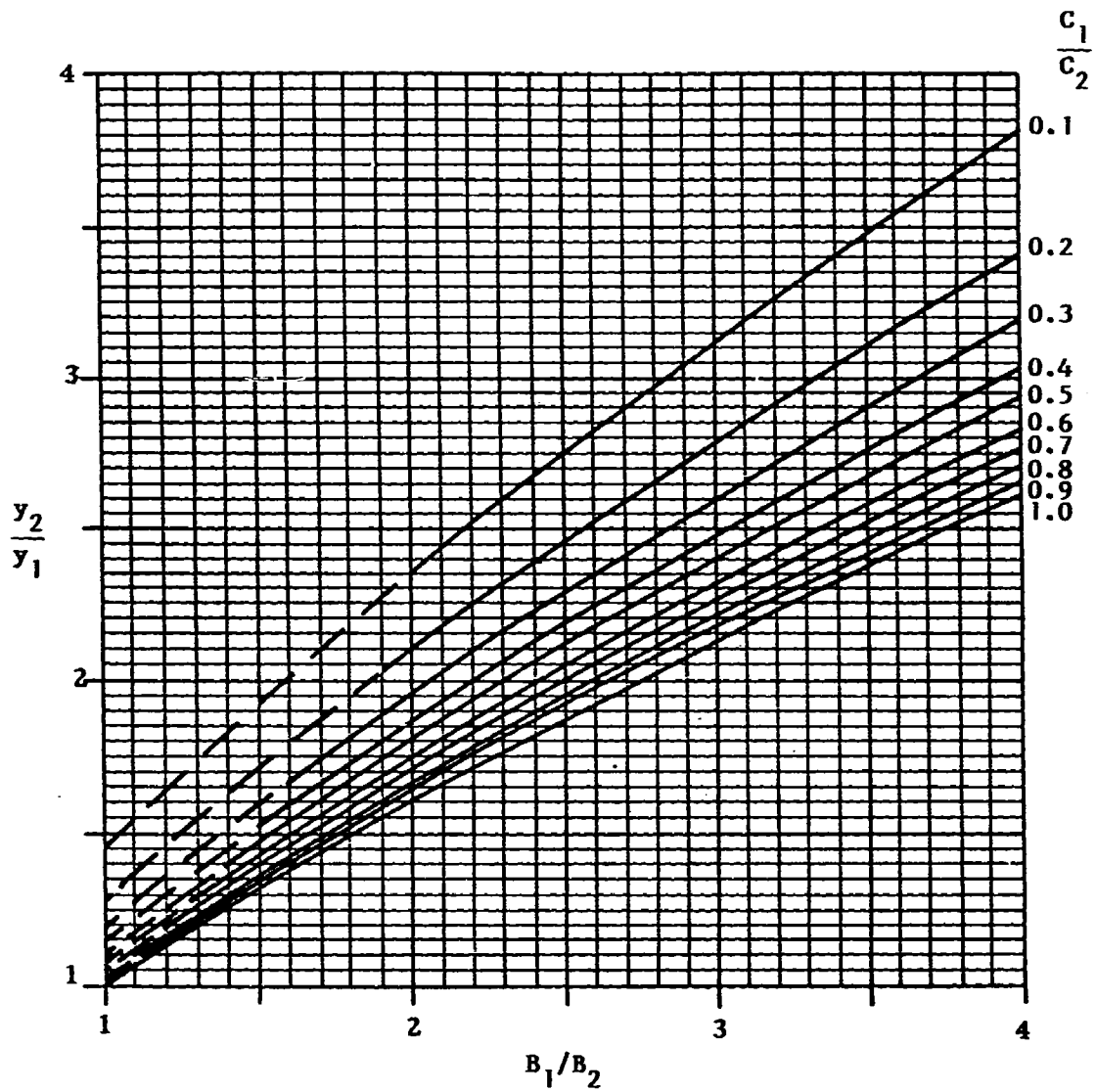


Figure 6. Depth Ratio vs Width Ratio and Shear Factor for Mostly Suspended Load in a Long Contraction.



To put this velocity effect in perspective, consider four streams all with depth of five feet and bed material of 0.02 feet (1/4 inch), and a contracted reach just half of the width of the approach reach. The first stream has a very, very high velocity and a depth in the contraction of 7.53 feet. The second has a shear ratio of 10, a velocity of 12.3 fps, a Froude number of 0.79, and depth in the contraction of 7.60 feet --only one percent more. The third has a shear ratio of 1.1, a velocity of 4.1 fps, a Froude number of 0.32 and a depth in the contraction of 8.75 feet -- still only 16 percent more. The fourth has a shear ratio of 1.0, a velocity of 3.88 fps, a Froude number of 0.31, and a depth in the contraction 9.43 feet -- 25 percent more than the limiting sediment-transporting case.

This example illustrates the point that with everything except the velocity kept constant, the depth (and scour) in the contraction increases with an increase in velocity until the sediment starts moving in the approach reach, and then the depth (and scour) decreases with further increase of the velocity, asymptotically approaching a limiting value. The example is a little contrived because the four streams probably cannot be found. If these are all streams in flood, it would be found that the sediment size in the slow-moving streams would be much finer than that of the fast-moving streams. For streams in flood, the shear ratio will almost assuredly be so high that the limiting solution is sufficient for practical

purposes -- especially if discharge and depth, etc. have been evaluated a trifle conservatively. Moreover, the ratio of the total shear velocity to fall velocity also has an effect on the depth of scour as do the velocity heads and losses.

The mode of movement changes from bed load only to some suspended load to mostly suspended load, as the shear velocity/fall velocity ratio changes from less than 1/2 to unity to greater than 2 (according to the Laursen sediment-transport relation). The sediment-transport dependence on the shear velocity/fall velocity ratio also changes, and the exponents of the independent parameters determining the depth ratio change slightly (Eqs. 17, 19 and 21). The extreme of mostly suspended load will result in a depth of flow in the contraction a little over seven percent more than the condition of bed load only. This effect tends to compensate for the previous effect that was associated with velocity and sediment transport. Note, however, the fall velocity is that of the material being scoured out, not the fall velocity of the fine fraction of the suspended load which would be sampled.

In all of these examples of how velocity can seemingly affect the scour process, it is not the velocity in itself which affects the scour, but rather something else which can be shown to be related to the velocity (such as particle shear or total shear velocity). Moreover, the velocity or velocity-related variable is contained in a dimensionless parameter or ratio such that if other things vary together with the velocity

in such a way that the parameter does not change, there is no apparent velocity effect on the scour.

There is one way, however, in which the velocity can have a more direct effect on the scour in a long contraction. This comes about in the definition of the depth of scour. The depth of scour needs to be defined differently, depending on the problem involved. A common definition in the case of the long contraction when the question is, "How much will the bed scour for some given rate of flow in a 'short' long contraction," is simply

$$d_s = y_2 - y_1 \tag{23}$$

If the Froude number is high (approaching or exceeding unity) this is not an adequate definition of the depth of scour. The difference in velocity heads and the loss in energy should also be considered in defining the depth of scour as shown in Figure 7. If the long contraction is long enough for the difference in slopes in the wide approach and the narrow contraction to be significant, this contribution to bed lowering should also be included.

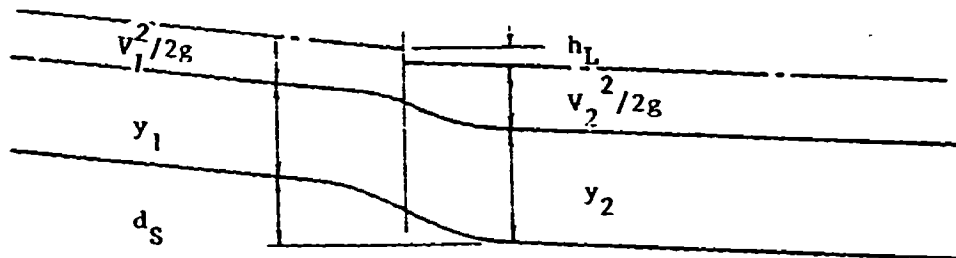


Figure 7. Definition of Depth of Scour for High Froude Number.

Extrapolating the conditions in the two reaches to the midpoint of the transition between the two, it is evident that

$$\frac{d_s}{y_1} + 1 + \frac{v_1^2}{2gy_1} = \frac{y_2}{y_1} + \frac{v_2^2}{2gy_1} + K_L \left( \frac{v_2^2}{2gy_1} - \frac{v_1^2}{2gy_1} \right) \quad (24)$$

If the head loss is taken as  $h_L = K_L (v_2^2/2g - v_1^2/2g)$ , a little algebraic manipulation will result in

$$\frac{d_s}{y_1} = \left( \frac{y_2}{y_1} - 1 \right) + \left[ \frac{1 + K_L}{2} \left( \frac{v_2}{v_1} \right)^2 - 1 \right] F_1^2 \quad (25)$$

For the case of bed load, a contraction to half the original width, and no energy loss, the inclusion of this velocity effect increases the scour by 75 percent at a Froude number of unity. With a loss of half the difference in the velocity heads, the increase in scour is over 100 percent. At a Froude number of 0.2, however, the increase in scour depth is only a few percent. It is interesting to note that at the downstream end of the long contraction the difference in elevation of the bed would decrease instead of increase with the inclusion of a loss term.

For other problems, and consequently other definitions of scour, the energy losses and velocity heads should similarly be included when the Froude number is high so that the "velocity effect" is significant. Note, however, that this analysis is for the long contraction, and that it is not necessarily transferable to the pier and abutment. The flow pattern in the

pier or abutment case is three dimensional, the velocity in the scour hole is about the same as in the approach (the "pressure" or piezometric gradient determining the scour hole velocity is due to the stagnation riseup of the approach velocity), the scour results from the boundary shear in the nonuniform flow, and any energy losses occur largely downstream of the scour hole as the horseshoe vortex mixes with the general flow.

#### ADAPTATION TO PIER AND ABUTMENT SCOUR

The solution of the scour in a long contraction was possible because the Manning equation and a sediment-transport relation along with the usual expressions involving continuity, boundary shear, critical tractive force, and Manning's  $n$  were sufficient to obtain equations for depth, slope, etc., in the contracted reach. The Laursen sediment-transport relationship was used, but other equations would give similar results; most of them very similar (13). Those which do not result in very similar expressions, predict behavior that does not seem to be quite reasonable. The reason most sediment-transport equations result in almost the same predicted scour in a long contraction is that relative, rather than absolute, rates of sediment transport are involved in the solution. Therefore, only the general form of the equation has to be approximately correct.

In order to obtain the solution for the scour at a pier or abutment in the same manner as for the long contraction, it would be necessary to be able to describe the flow pattern, the

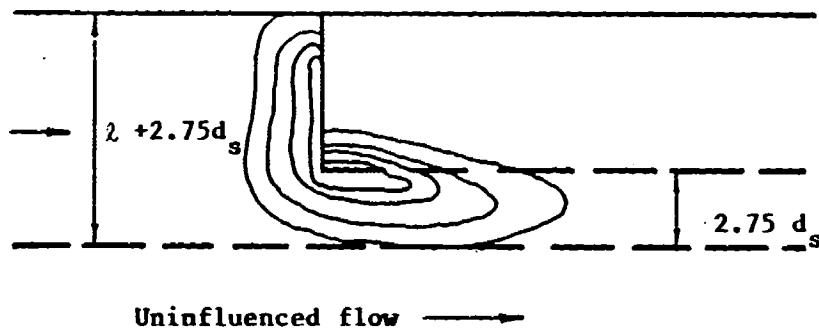
boundary shear pattern, and the sediment-transport pattern equally as well as it is possible to describe these characteristics of the total phenomenon in uniform flow. Fortunately, what cannot be solved in a straightforward manner can sometimes be solved with the aid of a trick or two -- or, more palatably, an assumption or two.

The observations that are needed in order to make some assumptions which serve that purpose are:

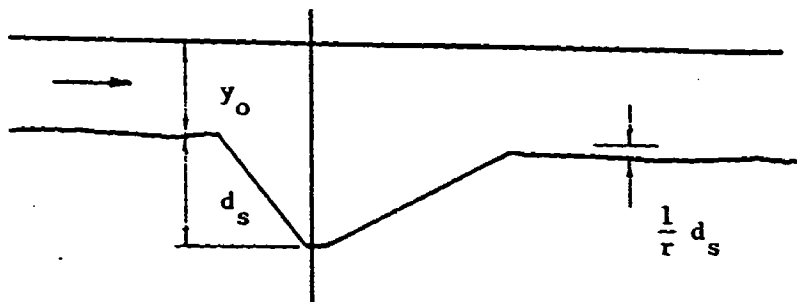
1. The flow and sediment being transported which are beyond the lateral extent of the scour hole behave as if the obstruction and scour hole were not there. (When the scour holes of adjacent obstructions -- either piers and/or abutments -- overlap, there will be some mutual interference; otherwise each obstruction and its scour hole is independent.)
2. The flow over the scour hole, but not obstructed by the pier or abutment, is virtually unchanged.
3. The flow obstructed by the pier or abutment dives into the scour hole, becomes a horseshoe vortex wrapped around the obstruction, and exits in a tail(s) downstream of the obstruction as it gradually mixes with the mainstream flow.
4. The front of the scour hole can be approximated as half of a truncated cone at the angle of repose. A pier at an angle to the flow can distort the cone, as can other geometry of the pier or abutment.

5. The sediment being transported moves straight ahead with the flow approaching the obstruction and scour hole, and falls into the scour hole.

The two key assumptions that can be made on the basis of these observations are that thin walls could be placed in the vicinity of the pier or abutment, as shown in Figure 8 to create a long contraction. In the case of the abutment, one



(a) Plan view



(b) Profile through scour hole

Figure 8. The Fictitious Long Contraction.

wall would be at the outside edge of the scour hole, and another wall would be downstream from the abutment at the end of the embankment. In the case of the pier, a third wall is needed through the centerline of the pier. The width of the approach reach is then

$$B_1 = l + 2.75 d_s$$

and the width of the contracted reach is

$$B_2 = 2.75 d_s$$

where  $2.75 d_s$  is the lateral extent of the top of the scour hole measured out from the side, or end, of the pier or abutment, and  $l$  is the half-width of the pier ( $b/2$ ), or the effective length of the embankment-abutment

$$l = \frac{Q_o}{V_o y_o}$$

where  $Q_o$  is the discharge being obstructed on the appropriate floodplain or in the portion of the channel being encroached upon, and  $V_o$  and  $y_o$  are the velocity and depth of flow in the channel approaching the river side of the scour hole. For very large actual embankment lengths, the pattern of the obstructed flow may not be well described by this simple notion of effective length. A better evaluation of the overbank flow as it approaches the bridge opening requires a two-dimensional flow analysis and detailed knowledge of the geometry and vegetation of the floodplain. At this extreme situation, the flow might return to the channel well upstream of the opening,



or it might return to the channel as a confined stream flowing parallel to and upstream of the embankment (depending on the path of least resistance to the flow).

The coefficient 2.75 was obtained from measurements taken in the Iowa experiments. If the bed material has an angle of repose steeper than those sands, the coefficient would be smaller; if flatter, larger. The angle of repose would have to change considerably to make a significant change in the depth of scour that would be predicted. A steeper angle of repose results in a deeper scour because less sediment is supplied to the scour hole.

The depth of scour in the fictitious long contraction can be obtained by using these two widths and the definition of scour depth as the difference in the flow depths of the two reaches. However, this is not the scour depth desired and a second assumption is needed. The scour depth desired is the scour at the pier or abutment, and the assumption is made that this scour is a factor  $r$  times the scour in the fictitious long contraction. A little algebraic manipulation will result in the following expression for the bed load case with  $r = 11.5$

$$\frac{l}{y_0} = 2.75 \frac{d_s}{y_0} \left[ \frac{C_1}{C_2}^{0.44} \left( \frac{1}{11.5} \frac{d_s}{y_0} + 1 \right)^{1.69} - 1 \right] \quad (26)$$

For a river in flood,  $C_1/C_2$  should be close to unity and this term can be dropped from Eq. (25). The coefficient 11.5 is the ratio of the scour at the pier or abutment to that in

the fictitious long contraction for the condition that the velocity of the flow being obstructed is about equal to the velocity of the flow approaching the scour hole and supplying sediment to the scour hole. Figures 9 and 10 display Eq. (26) for  $C_1/C_2 = 1$  for the embankment-abutment which encroaches into the channel and for the pier, respectively. This solution is for a rectangular pier aligned with the flow or a vertical wall embankment-abutment. For other shapes, multiplying factors to reduce the predicted scour for different geometry are given in Tables 1 and 2.

Table 1: Multiplying Factors for Piers Aligned with the Flow

Nose Form	Length/Width Ratio	$K_S$
Rectangular		1.00
Semicircular		0.90
Elliptic	2:1	0.80
	3:1	0.75
Lenticular	2:1	0.80
	3:1	0.70

Table 2: Multiplying Factors for Abutment Type For Small Encroachment Length

Abutment Type	$K_S$
Vertical Wall	1.00
45° Wing Wall	0.90
Spill-Through	0.80

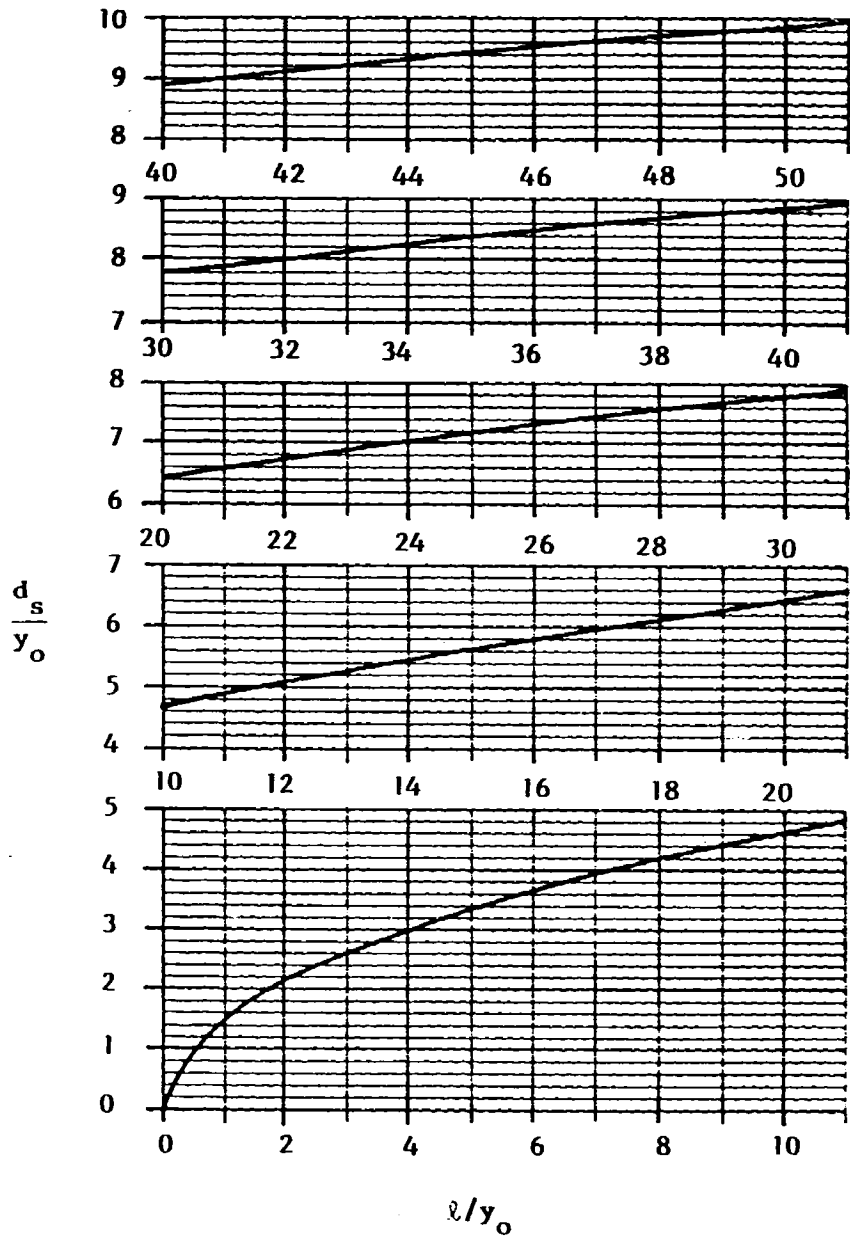


Figure 9. Scour Ratio for Encroaching Embankment-Abutment.

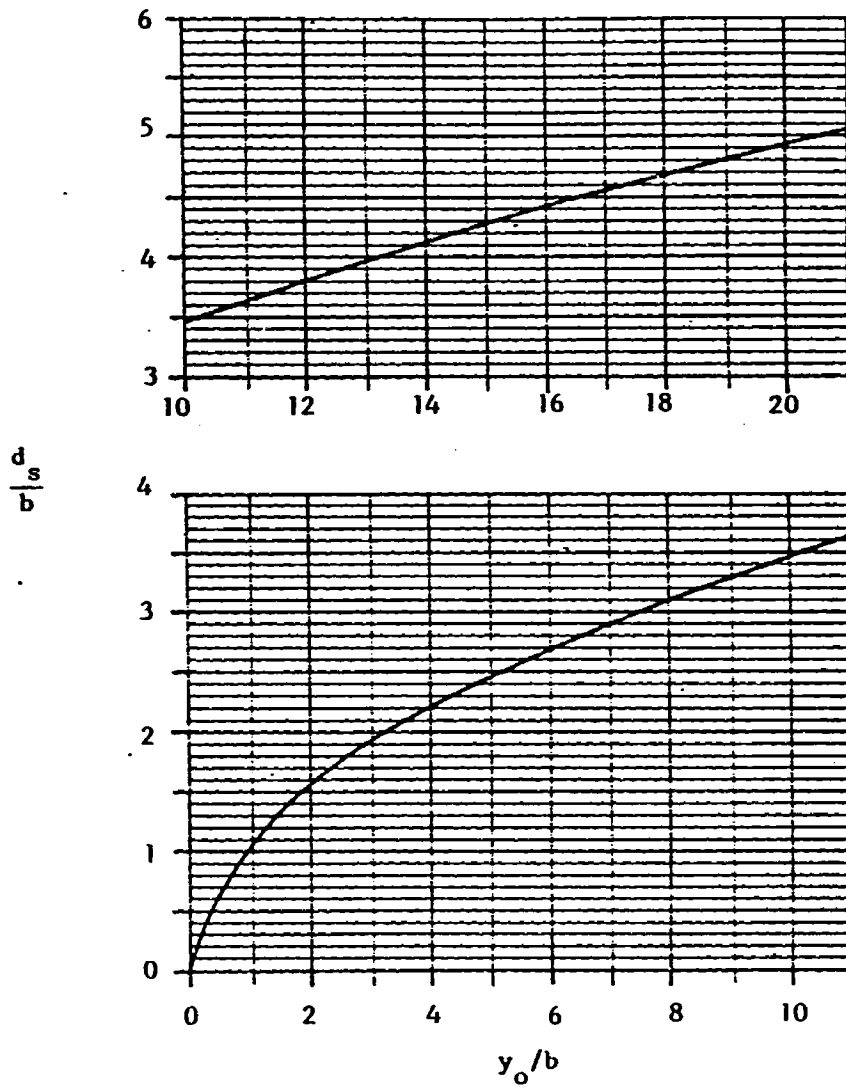


Figure 10. Scour Ratio for a Rectangular Pier Aligned with the Flow.

If the pier is not aligned with the flow, a multiplying factor greater than unity from Figure 11 should be used and the shape factor from Table 1 should NOT be used. Although a round pier does not lose its shape effect as the flow direction becomes misaligned, even a short 1:1-1/2 ellipse loses most (but not quite all) of its shape effect. Two questions that do not (and can not) have completely satisfactory answers are, "What might be the angle of attack during the life of the bridge?" and "How much debris might accumulate during a large flood thereby changing the geometry?" The two questions can be combined if the pier is a line of caissons with a spacing which is not large.

In a like manner, if the bridge does not cross the river at right angles, the scour can be greater or less, depending on the angle of incidence being greater or less than 90 degrees as shown in Figure 12. Finally, there is another multiplying factor to be used if the mode of sediment movement is not bed load, but either some suspended load or mostly suspended load; the amount of suspension being a function of the shear velocity/fall velocity ratio as shown in Figure 13.

A similar adaptation will permit the solution of the embankment-abutment that obstructs low-velocity flow on a floodplain which is not carrying a sediment load of the size of the material which must be scoured. The predicting equation is

$$\frac{Q_o w}{Q_w y_o} = 2.75 \frac{d_s}{y_o} \left[ \left( \frac{1}{4.1} \frac{d_s}{y_o} + 1 \right)^{7/6} - 1 \right] \quad (27)$$

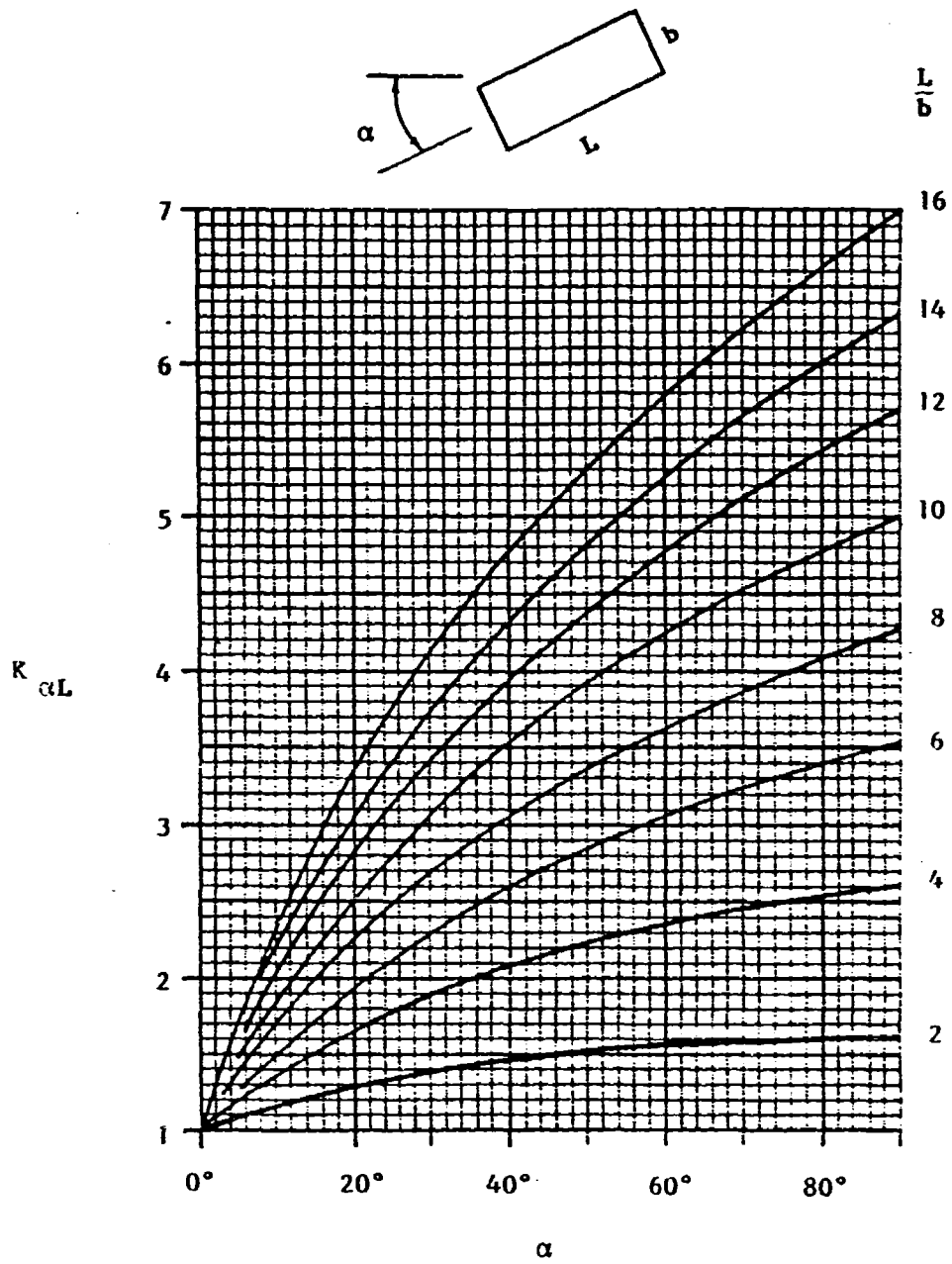


Figure 11. Multiplying Factor for Angle of Attack on Pier.

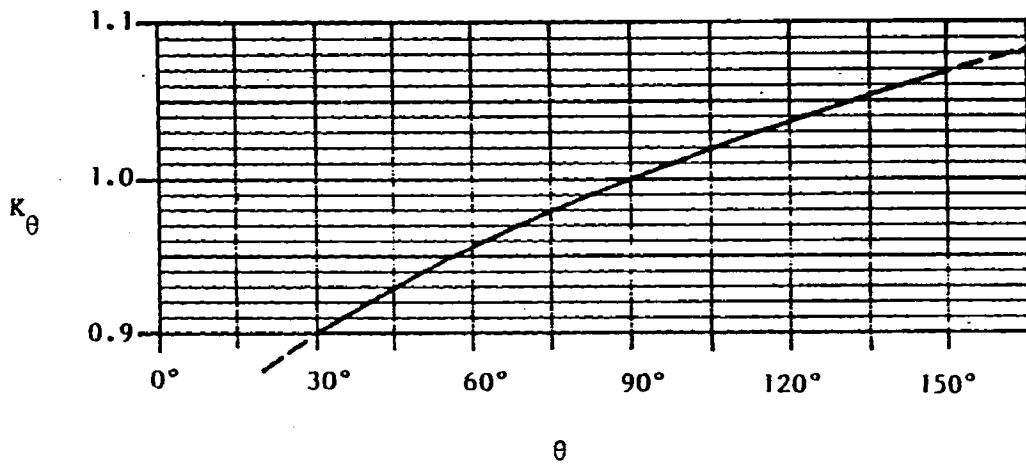


Figure 12. Multiplying Factor for Angle of Incidence of Encroaching Embankment-Abutment.

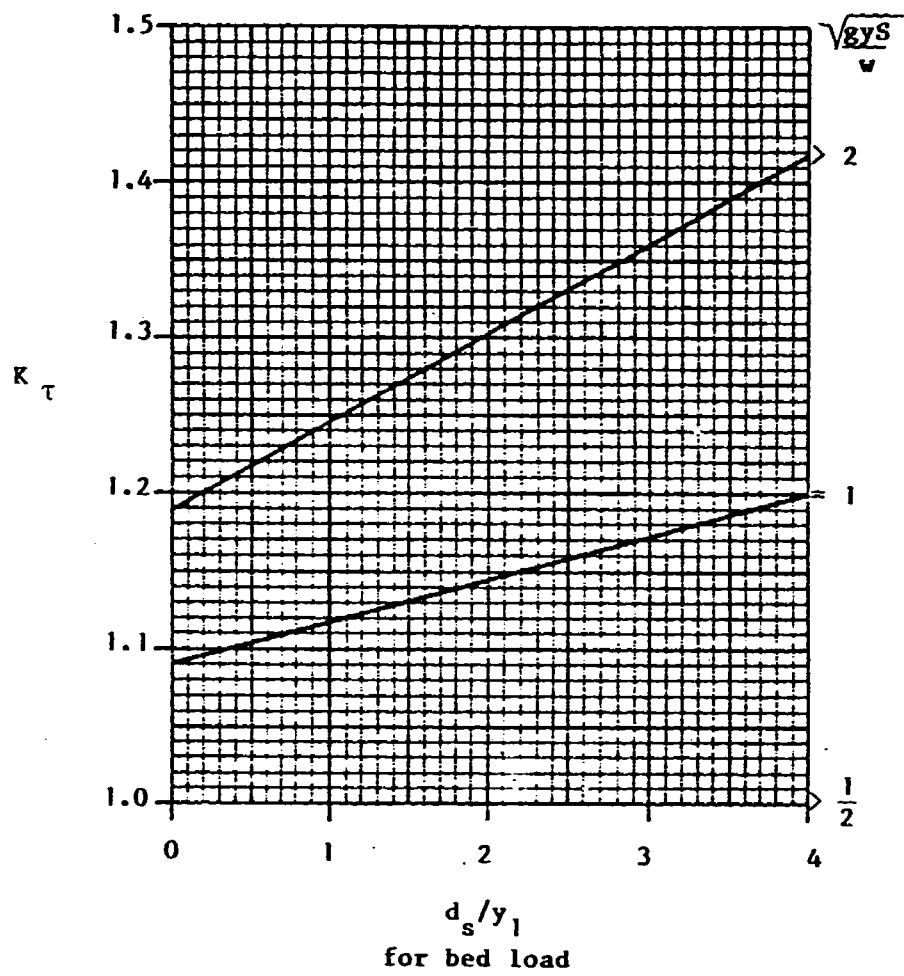


Figure 13. Multiplying Factor for Mode of Movement.



where the coefficient 11.5 is replaced by the value 4.1 (the obstructed flow is relatively low velocity),  $Q_o$  is the overbank flow being obstructed,  $w$  here is a width about equal to  $2.75 d_s$  and  $Q_w$  is the channel flow in the width  $w$  approaching the scour hole.

Equation (27) is shown graphically in Figure 14. The dashed line is meant to be a reminder that when  $Q_o$  is first evaluated as being small, it is a good idea to check again.

The case of clear-water scour can also be adapted to piers and abutments with the basic equation being

$$\frac{l}{y_o} = 2.75 \frac{d_s}{y_o} \left\{ \frac{\left[ \frac{1}{11.5} \frac{d_s}{y_o} + 1 \right]^{7/6}}{\left[ \frac{\tau_o'}{\tau_c} \right]^{1/2}} - 1 \right\} \quad (28)$$

The clear-water relationships for piers and abutments are shown in Figures 15 and 16. In real life this case is of little interest because in floods, rivers generally have a bed load. The relationships, however, can be used to size the riprap needed to stop the scour at some predetermined level that can be tolerated. This case is of greater interest for old existing bridges than for bridges being designed.

The critical assumption in using Eq. (28) for sizing riprap is that riprap of some size placed at some level below the streambed will stay in a flood and limit the scour depth to that level, and that the size of riprap and the placement level can be predicted as if the entire streambed was

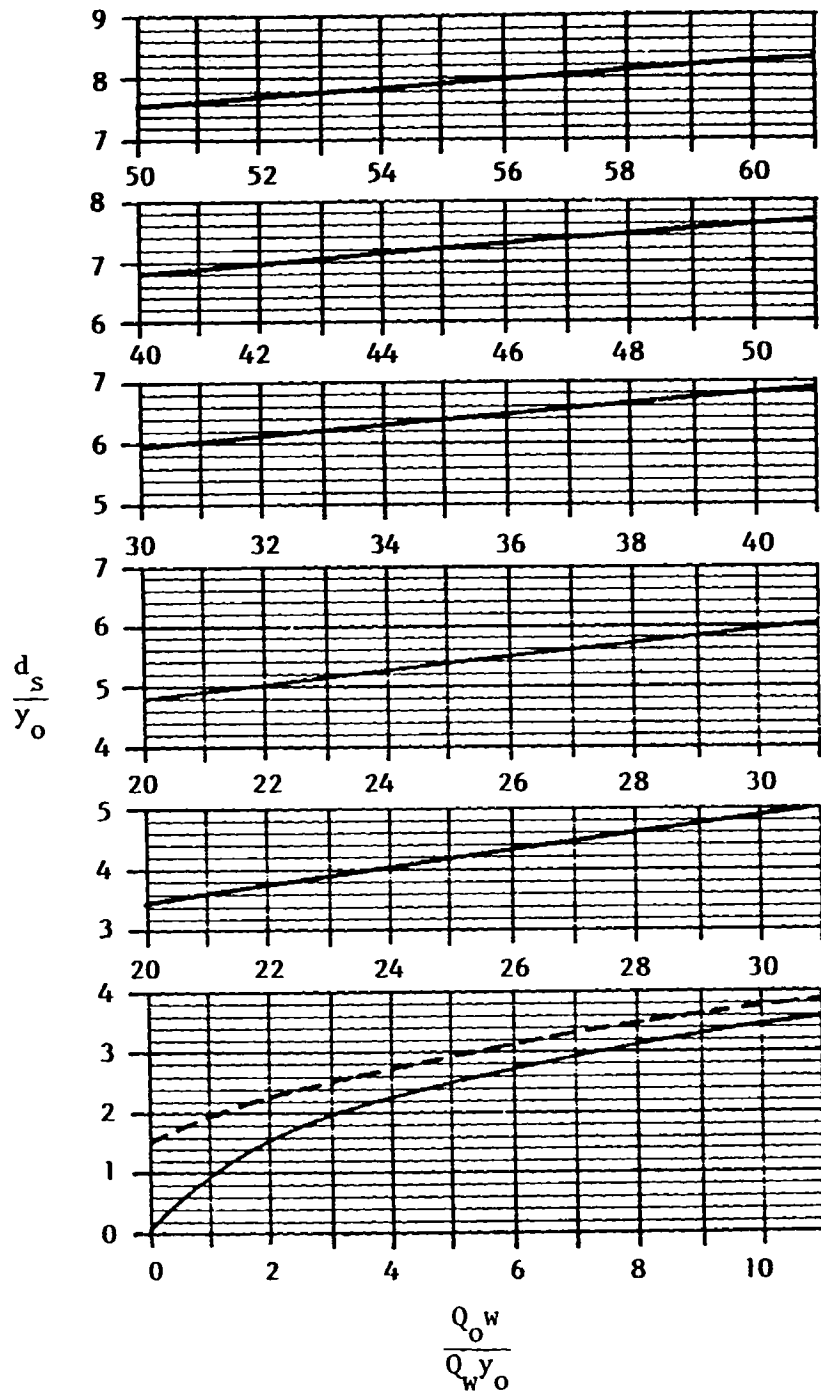


Figure 14. Scour Ratio for Floodplain Constriction.

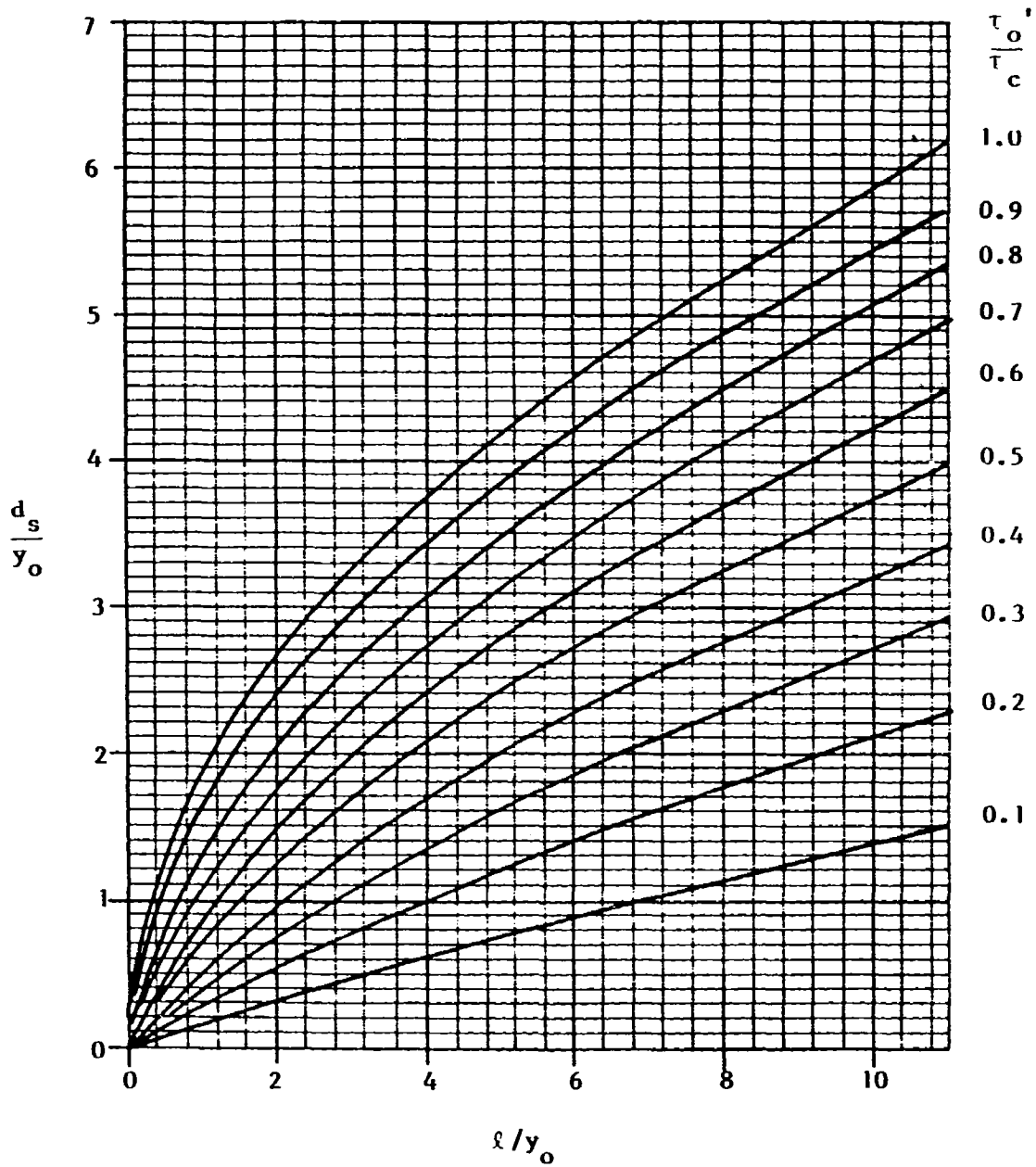


Figure 15. Scour Ratio for Encroaching Embankment-Abutment for Clear-Water Scour.

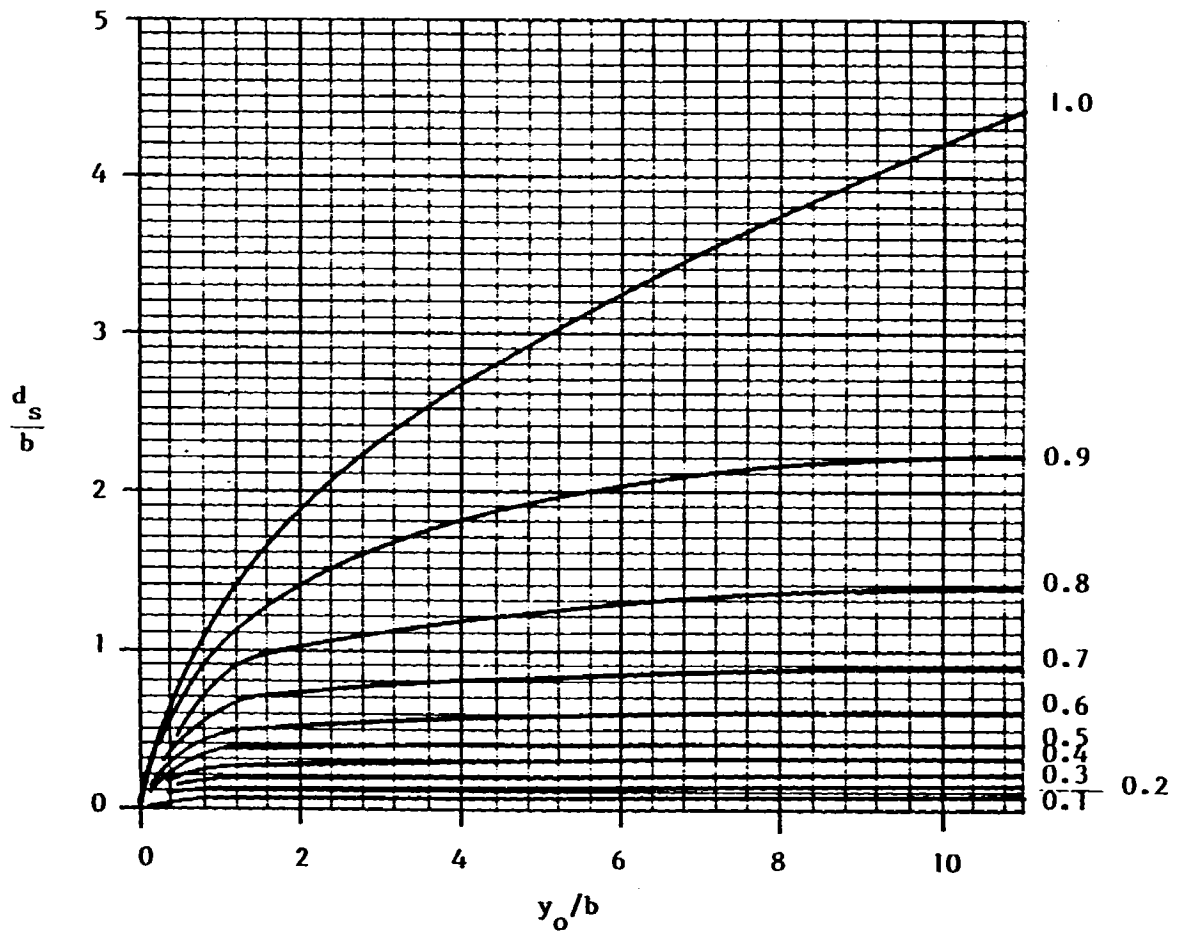


Figure 16. Scour Ratio for Pier for Clear-Water Scour.

composed of the riprap. Preliminary tests indicate this to be so -- surprisingly even without tampering with the coefficients for  $\tau'_0$  or  $\tau_c$  .

#### THE EXPERIMENTS

Two flumes were used in the investigation. For the investigation of the long contraction, the flume used was 100 feet long and 3 feet wide in the test section -- although a few feet at each end of the flume were discounted because of end effects. The narrow contracted reach was 30 feet long and 1.5 feet wide and centered slightly upstream of the midpoint of the flume. Transition sections at each width change were 10 feet long and composed of two circular arcs. Figure 17 is a photograph of the 100-foot flume.

The flume could be tilted to various slopes, but not during operation. At the head end, sand was supplied from a hopper through a flexible tube which traversed back and forth across the width of the flume. At very low rates of sand feed, the orifice in the bottom of the hopper was so small it would clog and hand feeding at the prescribed rate was necessary. At the highest rates of sand feed, the capacity of the flexible tube was exceeded even though a larger diameter tube was installed and hand feeding by bucket directly into the flume was resorted to. At the highest rate of sand feed, the trap at the tail end of the flume was filled in the time it took to get the readings for the water-surface and bed profiles at two-foot intervals.

Elevations were taken with a point gage fastened to a carriage riding on rails on the wall behind the flume. In supercritical flow, the "sinusoidal" waves over antidunes made

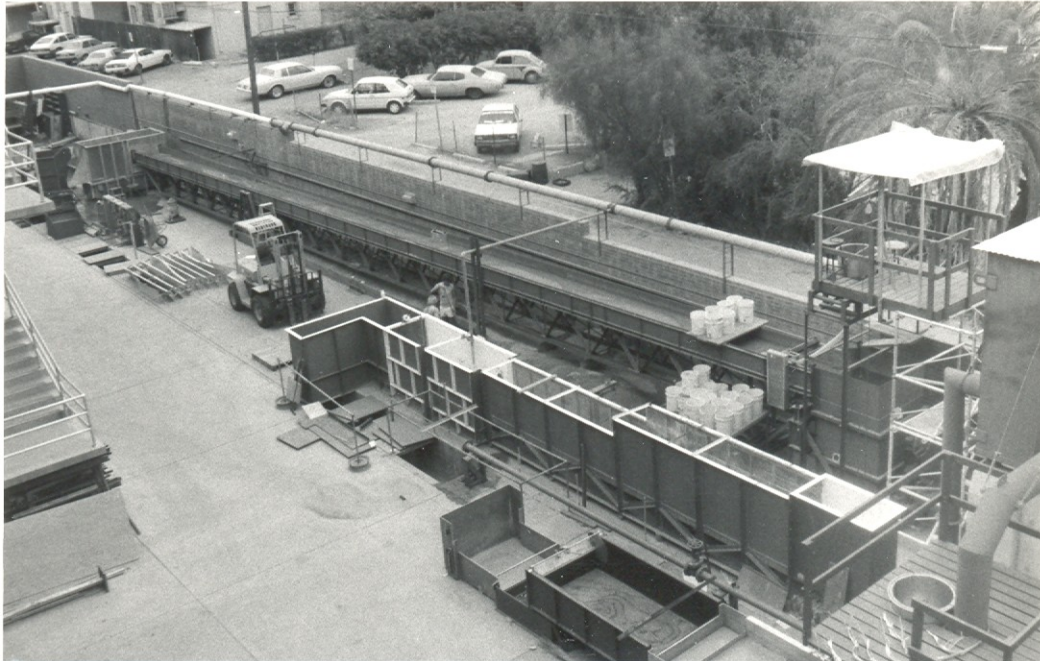


Figure 17. One-Hundred Foot, Long-Contraction Flume.

the water surface very difficult to measure. These waves were especially strong in the transition from the narrow, contracted reach to the normal, wide reach downstream. Elsewhere the train of waves tended to shift from side to side and to come and go. For this condition, the profiles were taken on a line just inside of the wall of the contracted reach in order to minimize the height of the waves.

The point of the point gage was replaced with a half-inch cylinder for the measurement of bed elevation. Positioning of the gage was a matter of feel as much as sight. Especially at higher velocities, a small scour hole could develop as the cylinder approached the bed. Therefore, it was necessary to set the gage on the bed quickly, but not so quickly as to drive the cylinder into the bed. There was probably a systematic error with the measured bed elevations slightly low. However, it is not believed that this error is significant. The possible errors due to the wavy water surface and the ripples, dunes and anti-dunes are larger, but by averaging, the values of depth and slope are sufficiently accurate for the purpose of the study. The values of depth, which are of primary interest, are more reliable than the values of slope.

The smaller flume was only 10 feet long but was 4 feet wide, and could accommodate a vertical wall abutment on one side and a rectangular half-pier on the other side. The flume had the same arrangement for sediment supply at the head end, a trap at the tail end, and a weir for measuring the discharge. This flume is shown in Figure 18.

The abutment model was a vertical wall nominally 6 inches by 12 inches which actually encroached into the flow 6-1/4 inches. The pier half-model was 1 inch wide by 12 inches long. The scour holes around the pier were small and the approach conditions were not sufficiently uniform to be able to

obtain meaningful measurements. However, qualitatively the pier exhibited the same scour behavior as the abutment.

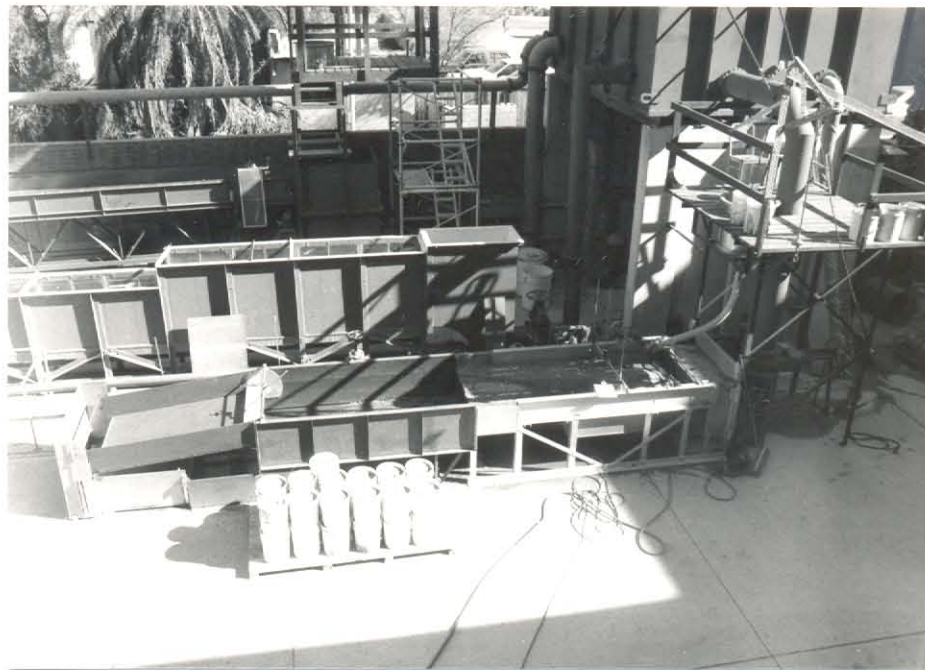


Figure 18. Pier-Abutment Flume.

Because the flume was so short, profiles were not taken, and the measurements simply established depth of flow, depth of scour, width of scour and, of course, discharge. The point gages, like those used with the 100-foot flume, were attached in this case to an angle which rested on the flume walls.

Two sediments were used in the experiments: a pea gravel with a mean size of 5.6mm and a sand with a mean size of 1.35mm. The size distribution of the two sediments are shown in Figure 19.



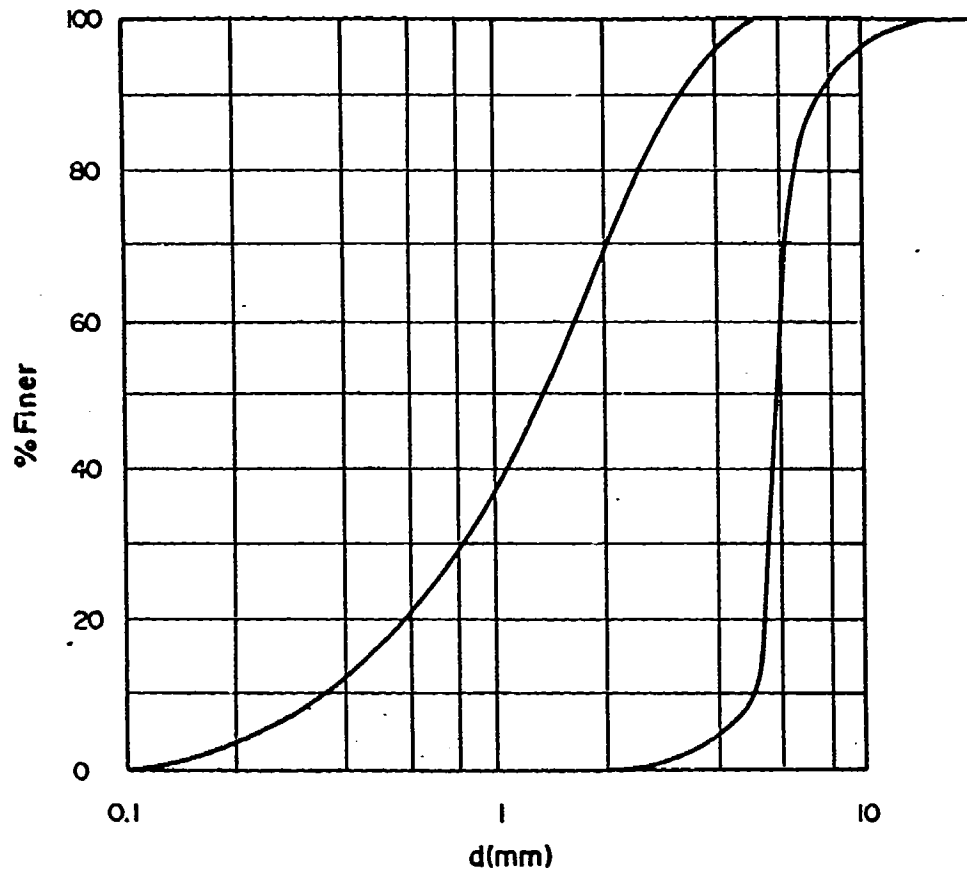


Figure 19. Size Distribution of Sand and Gravel.

## THE LONG-CONTRACTION SCOUR MEASUREMENTS

### General Findings

The water-surface and bed profiles, and the energy line are shown in Figures 20-42. Runs 1-13 (Figs. 20-31) were with the pea gravel as a sediment; Run 1 was a determination of the discharge when particles began to move in the contraction. Runs 14-23 (Figs. 32-40) were with the sand as a sediment; Run 14, like Run 1, was a determination of the discharge when particles began to move in the contraction. Runs 24 and 25 (Figs. 40 and 42) were runs with a 45° wing-wall abutment instead of the long contraction; the sediment being gravel and sand, respectively. The purpose of these last two runs was to measure the backwater behavior at a bridge opening with a supercritical flow.

The eye is not a precise enough measuring instrument and the approach depth was not always the same; nevertheless, several conclusions are possible on looking at these figures:

1. The depth of flow in the contraction is 50% (or more) greater than in the approach -- and does not change much as the discharge is increased, except in the clear-water case where it changes from zero to a maximum.
2. The slopes increase as the discharge (and, therefore, the velocity) is increased, and the slope in the contraction is somewhat less than the slope in the wider reaches.

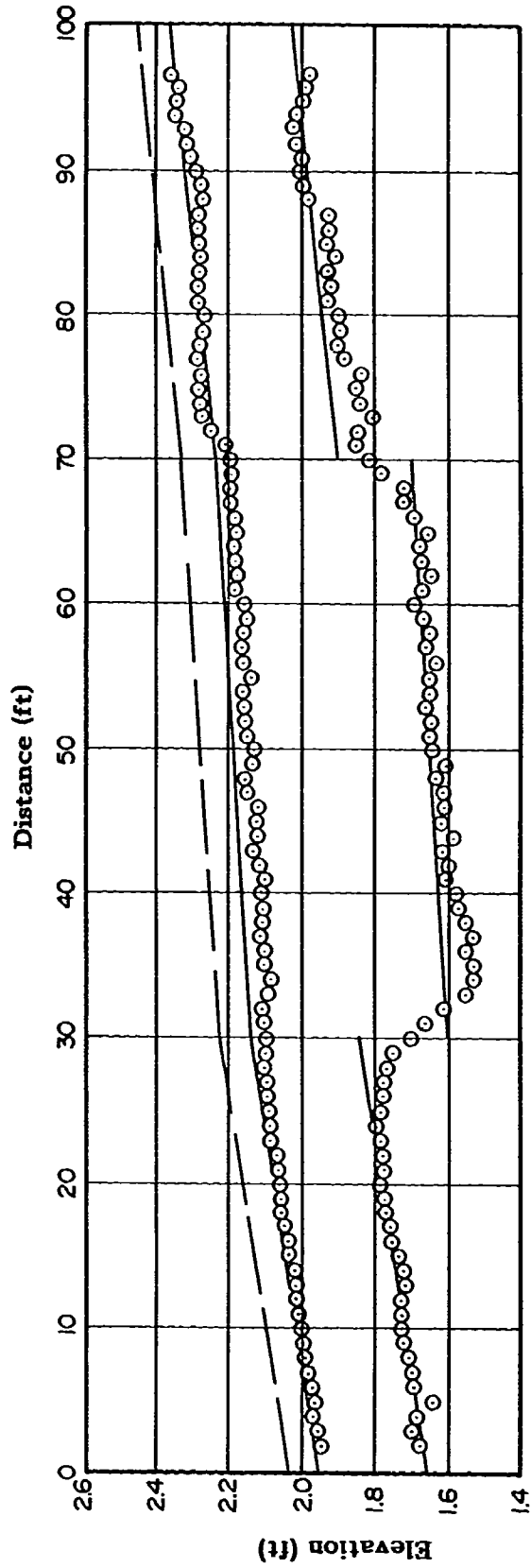


Figure 20. Profiles for Run No. 2.

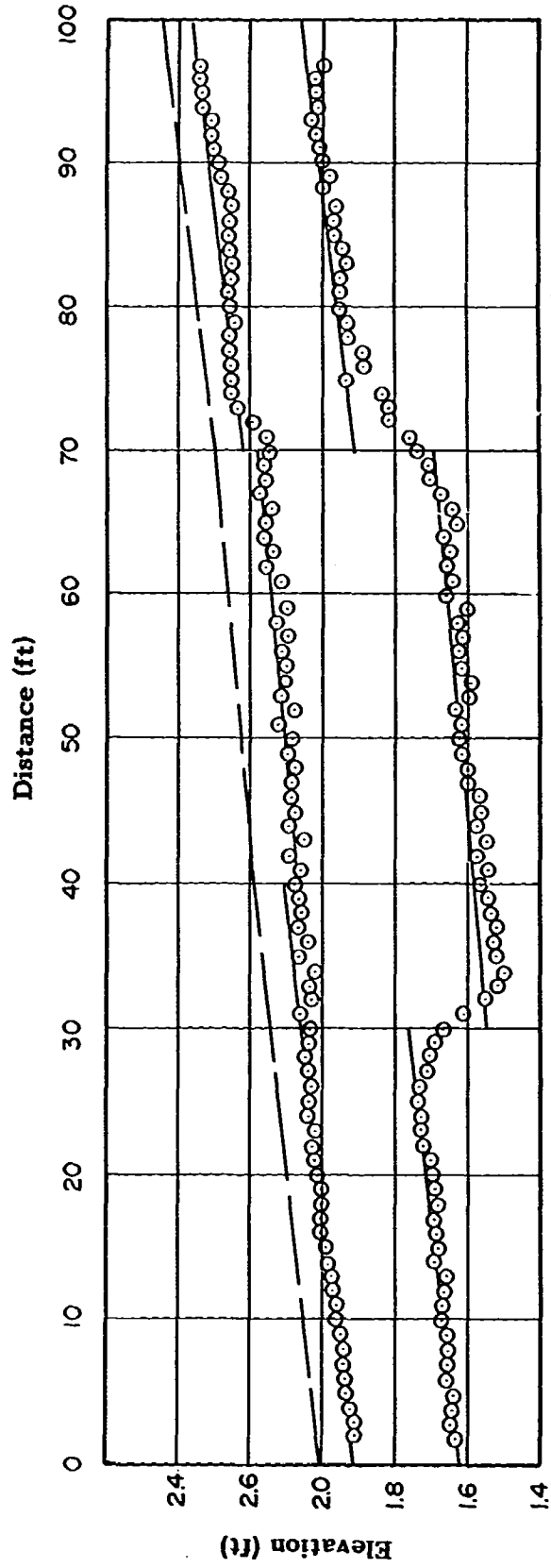


Figure 21. Profiles for Run No. 3.

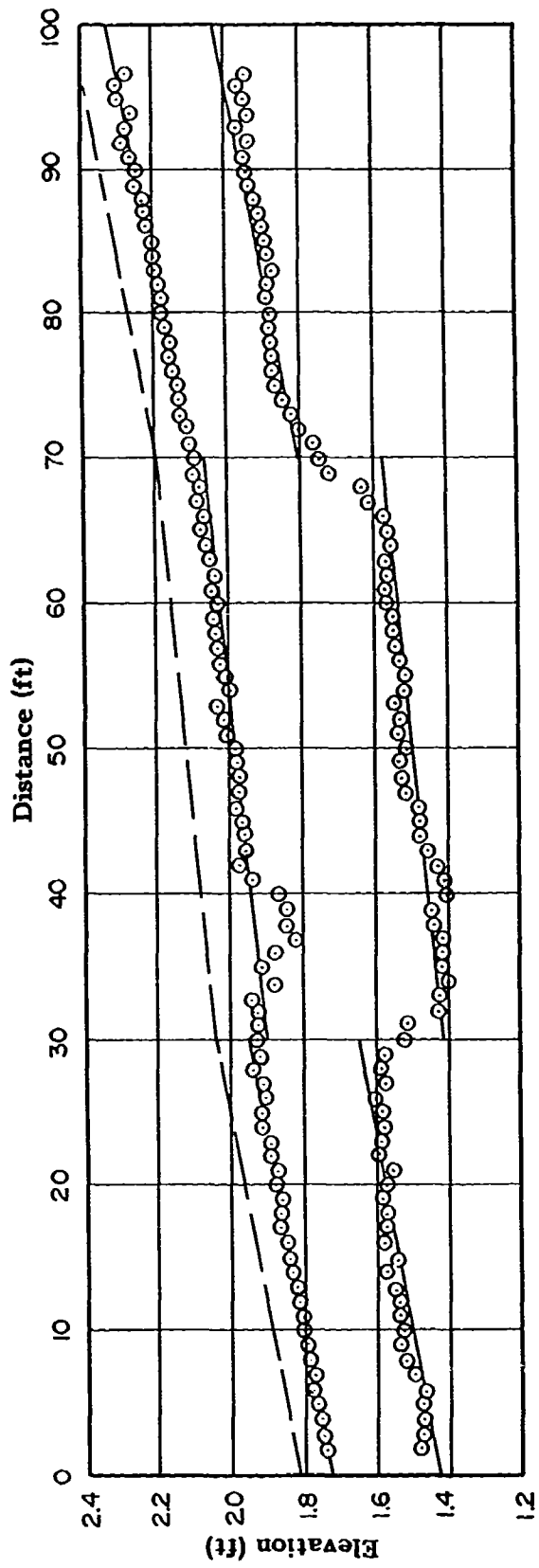


Figure 22. Profiles for Run No. 4.

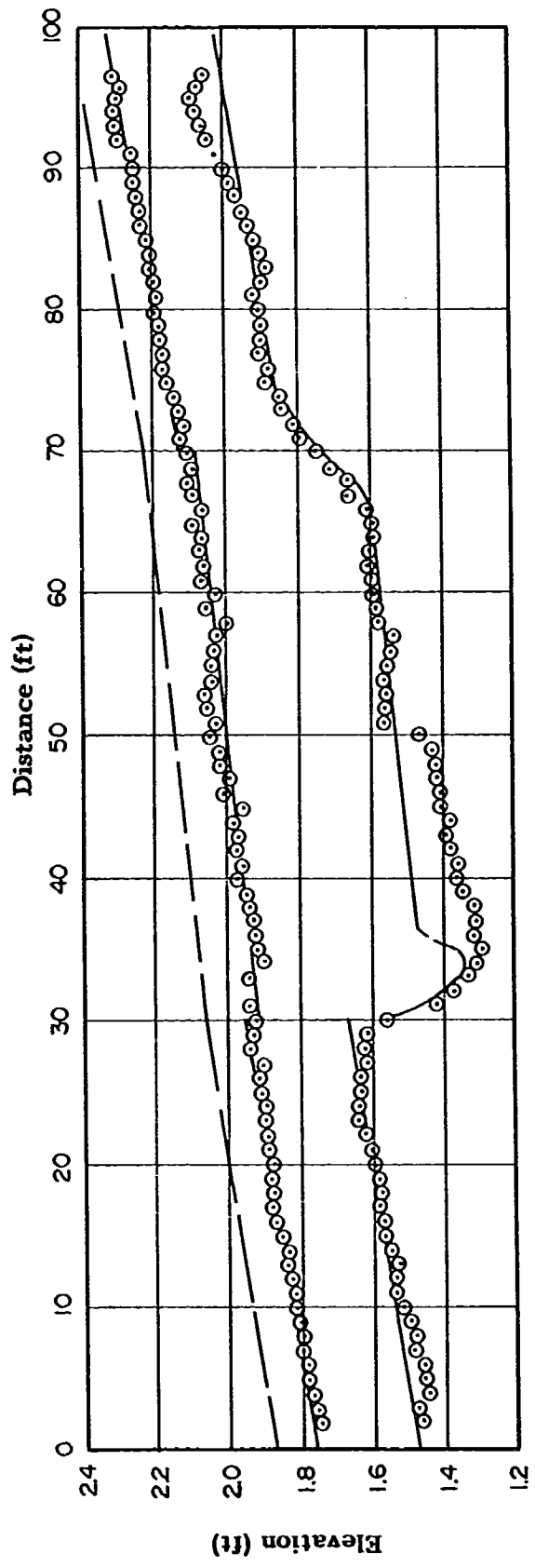


Figure 23. Profiles for Run No. 5.

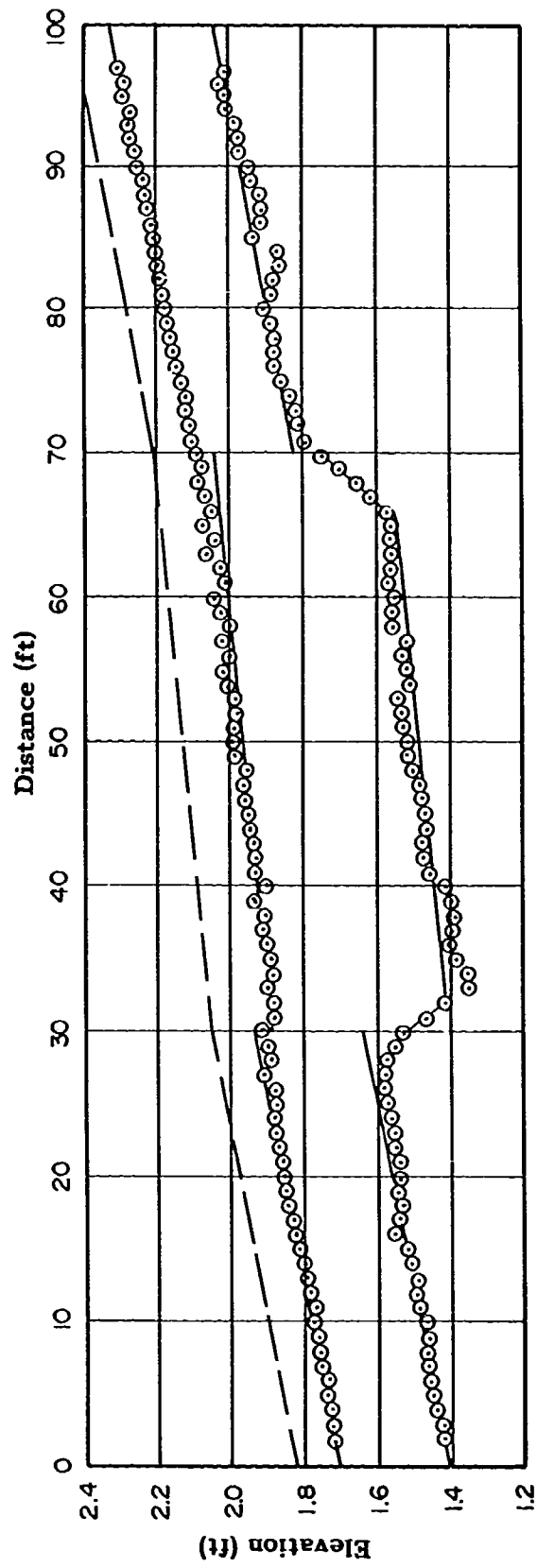


Figure 24. Profiles for Run No. 6.

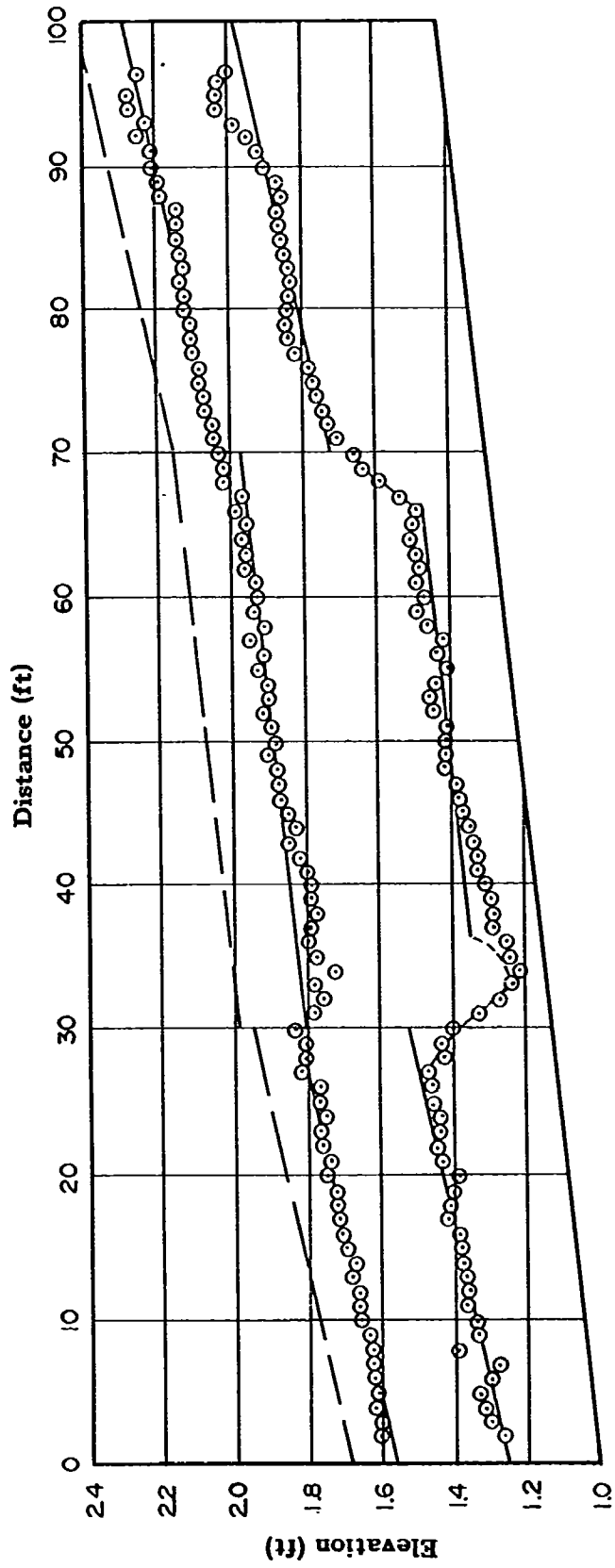


Figure 25. Profiles for Run No. 7.



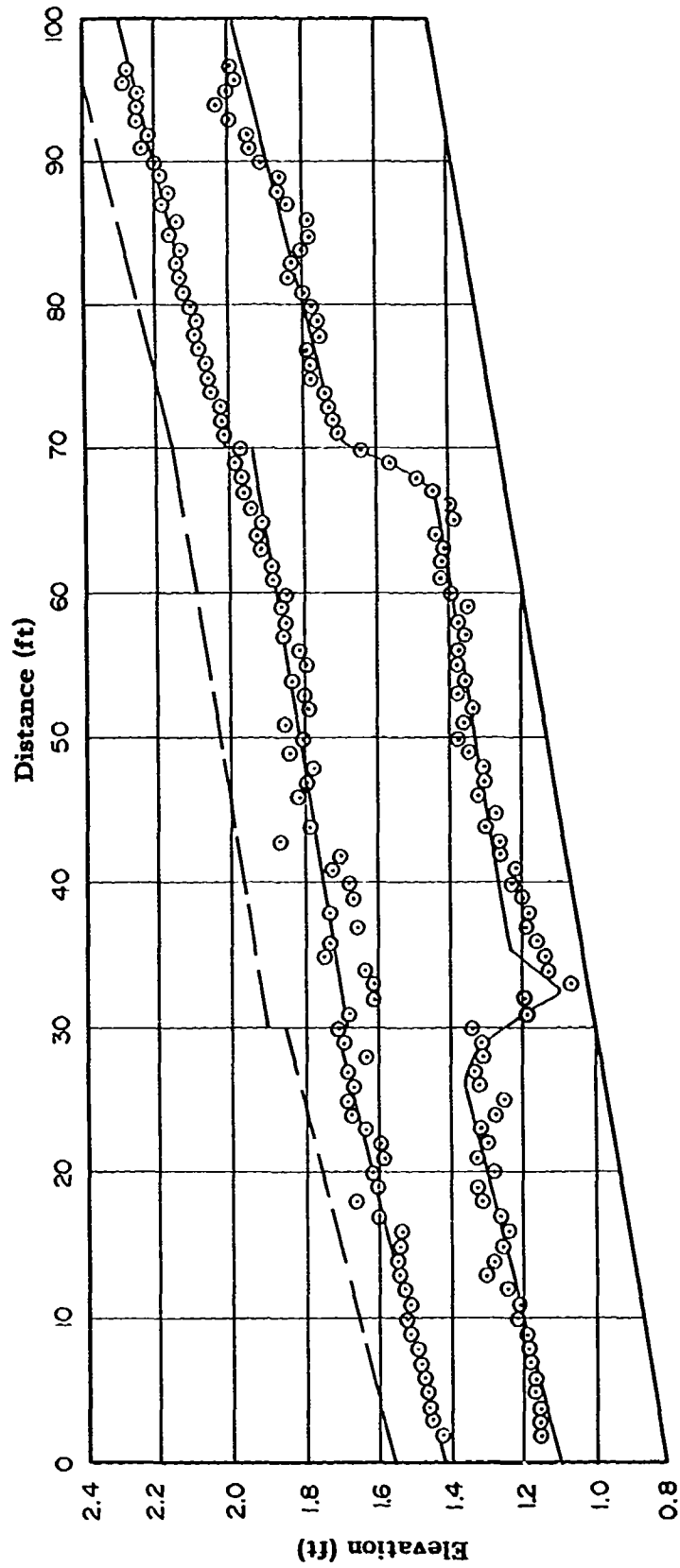


Figure 26. Profiles for Run No. 8.

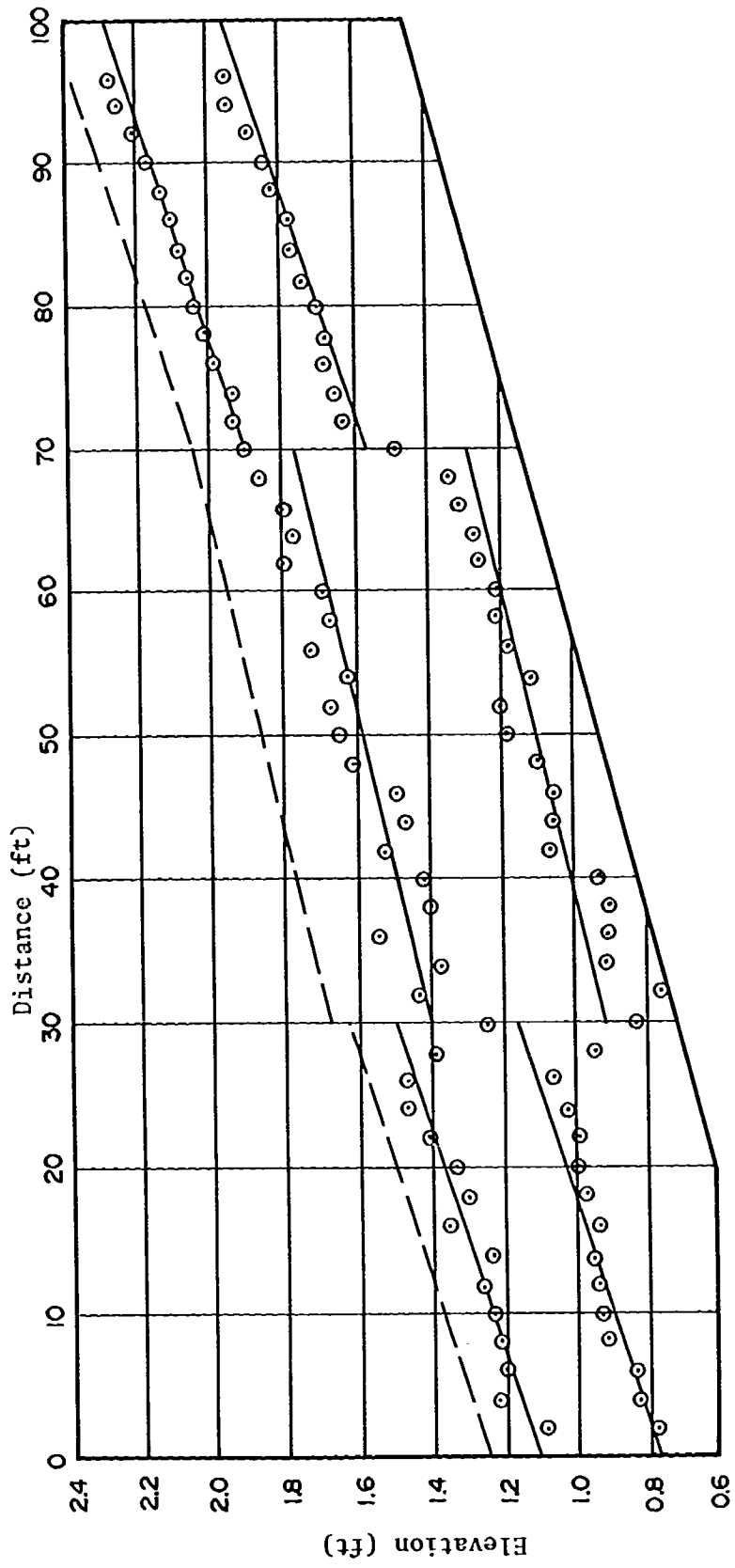


Figure 27. Profiles for Run No. 9.

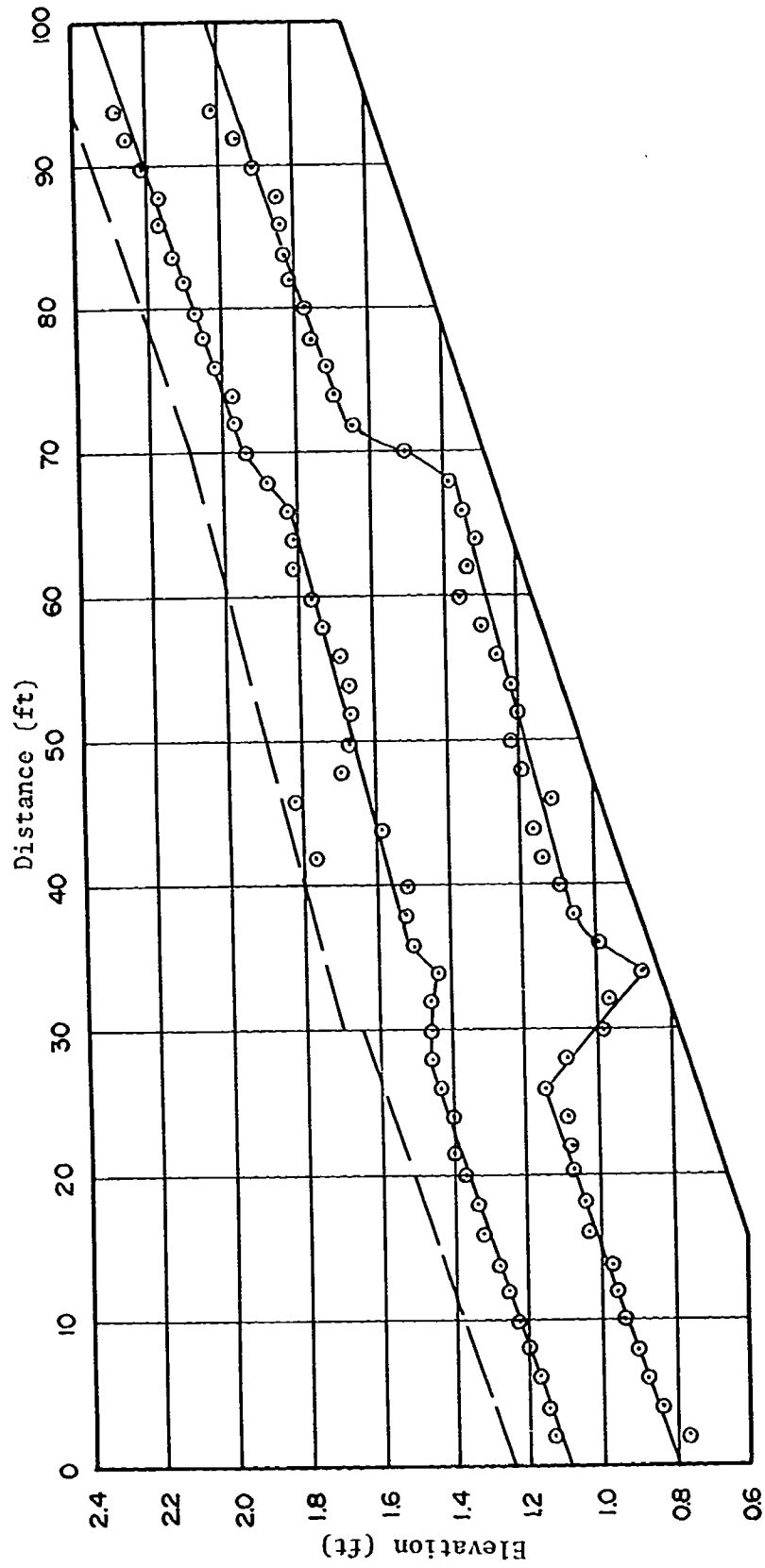


Figure 28. Profiles for Run No. 10.

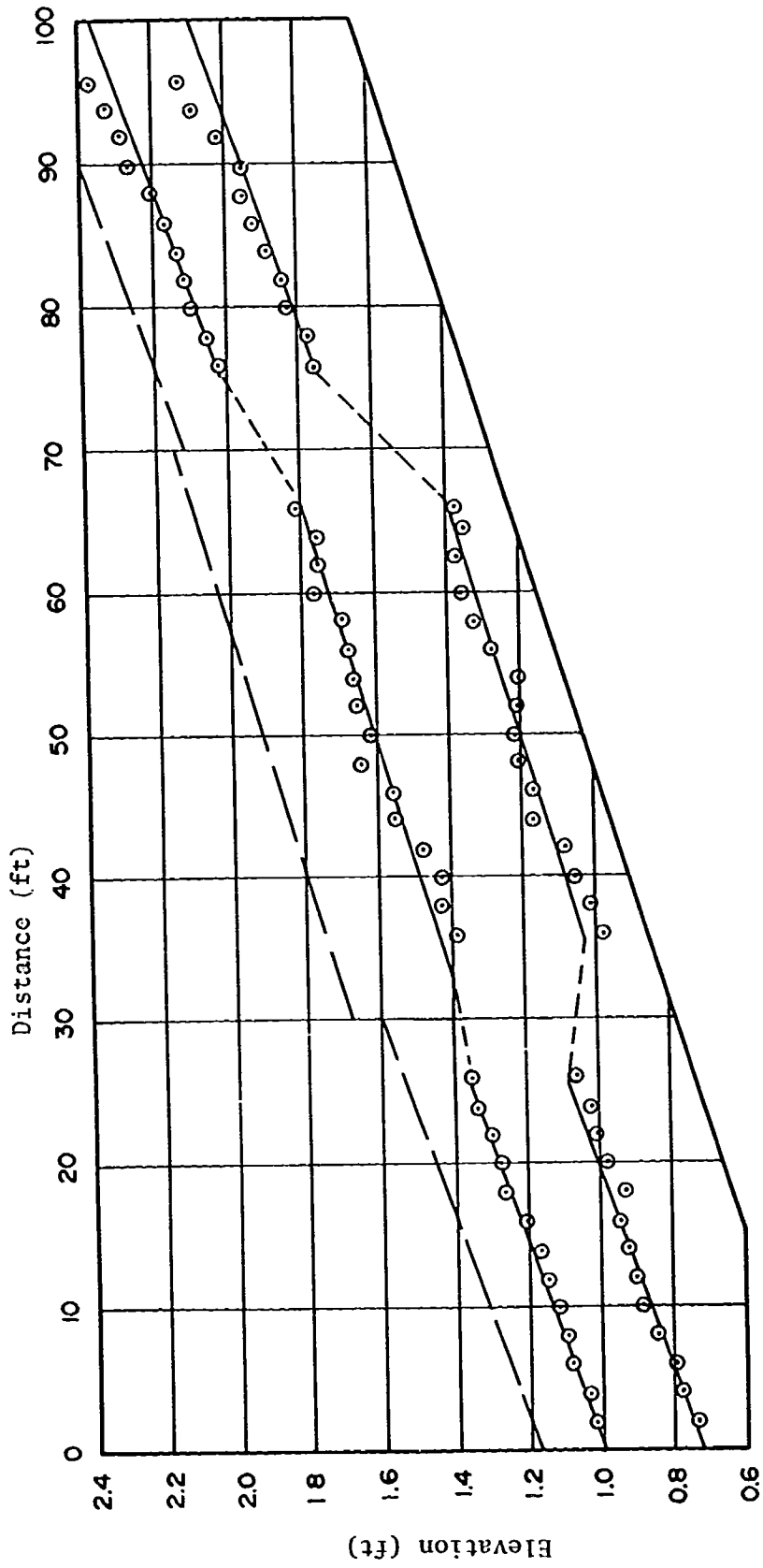


Figure 29. Profiles for Run No. 11.

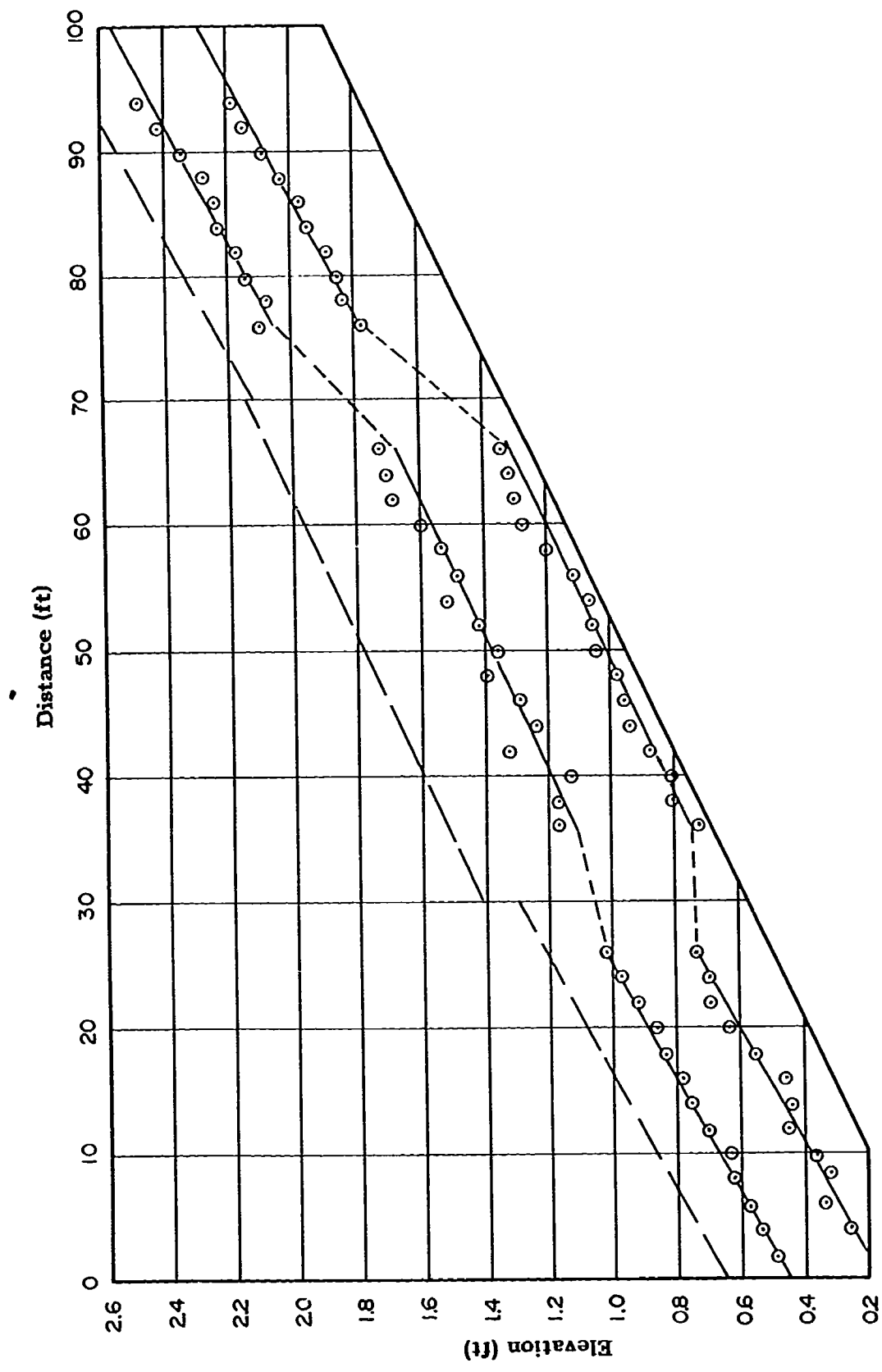


Figure 30. Profiles for Run No. 12.

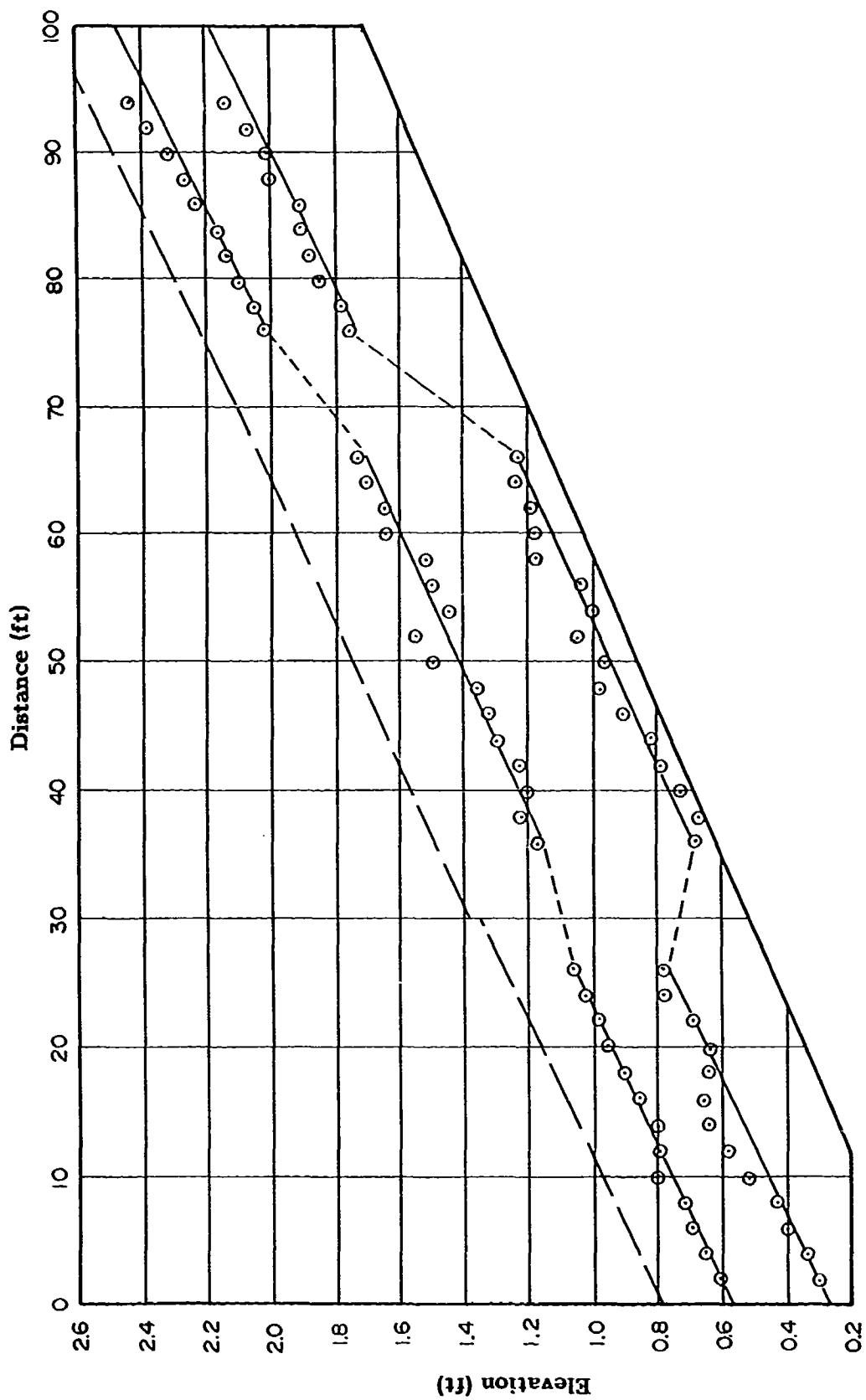


Figure 31. Profiles for Run No. 13.

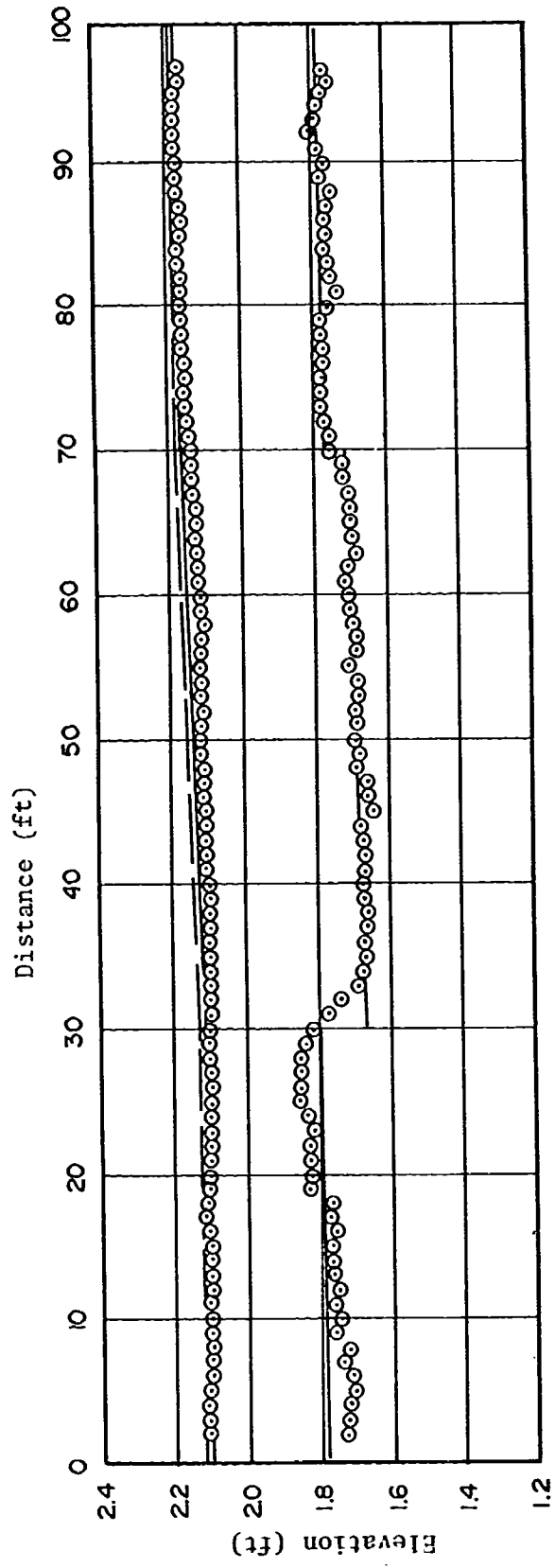


Figure 32. Profiles for Run No. 15.

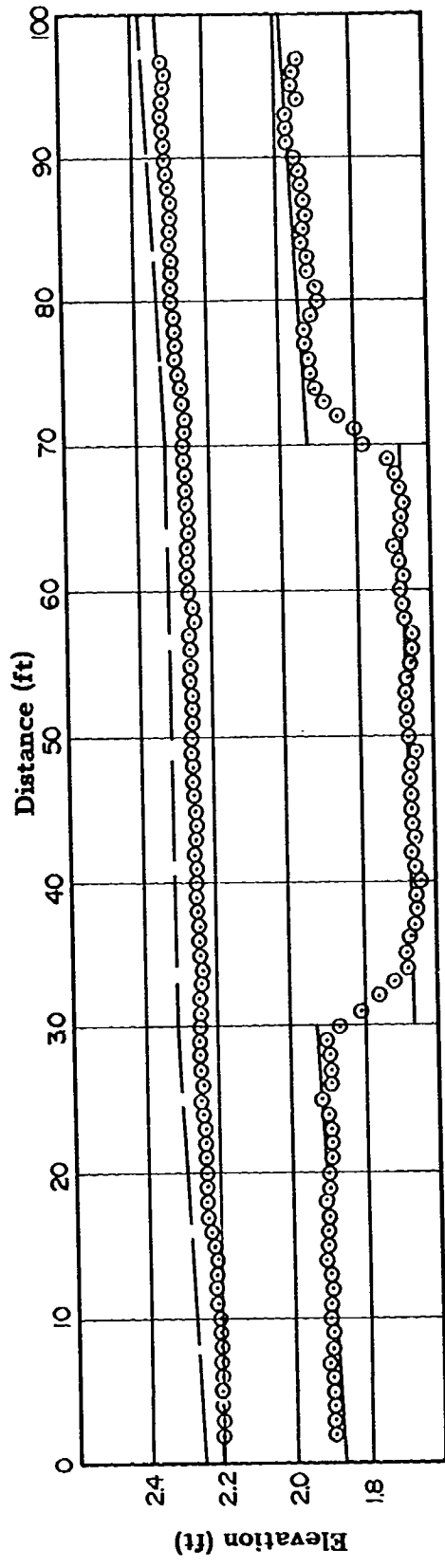


Figure 33. Profiles for Run No. 16.



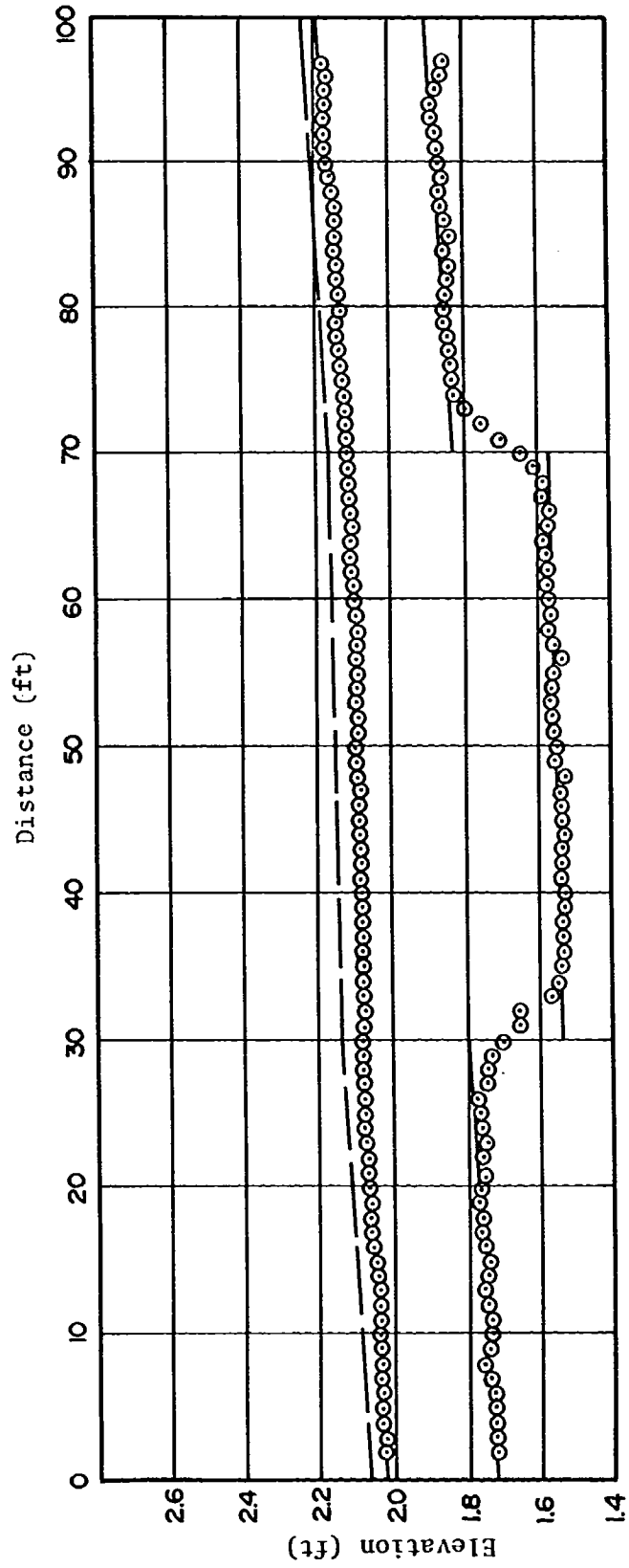


Figure 34. Profiles for Run No. 17.

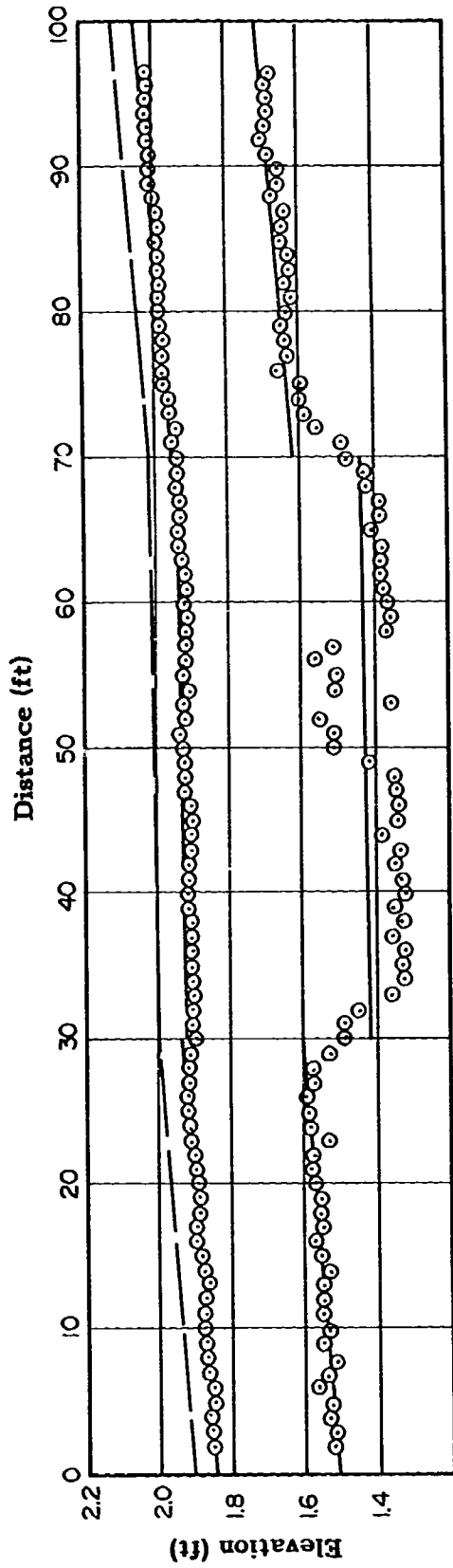


Figure 35. Profiles for Run No. 18.

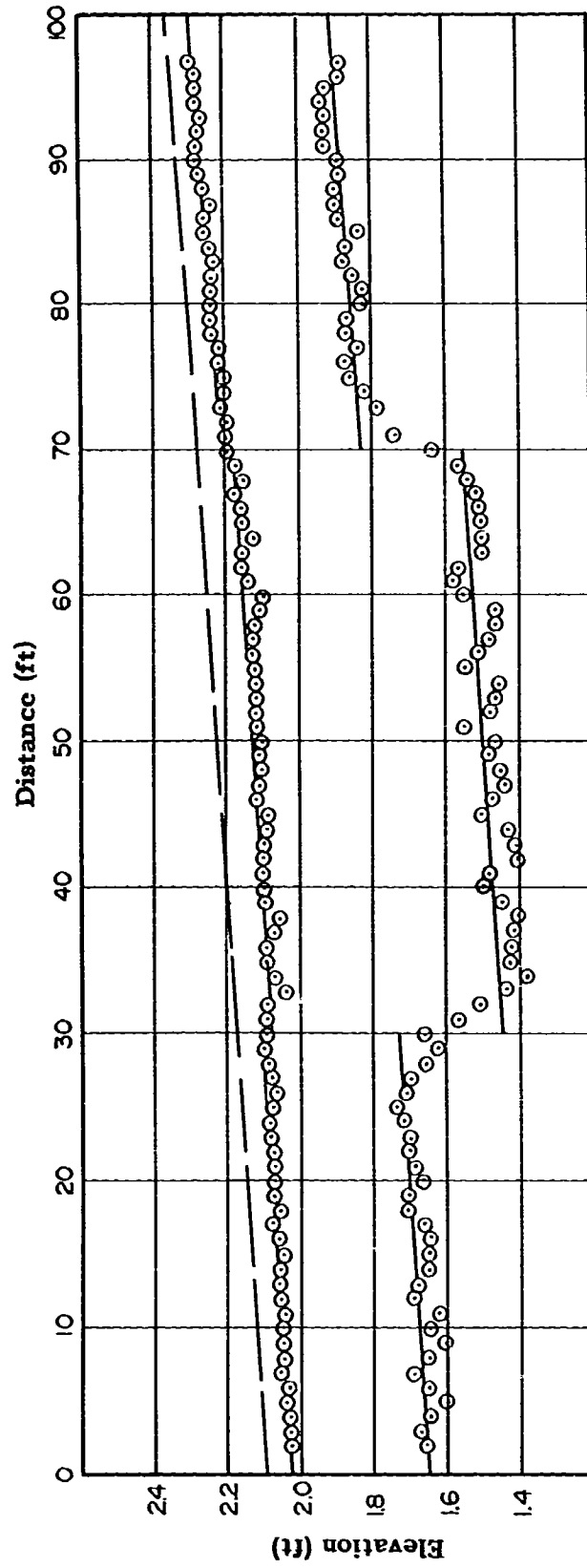


Figure 36. Profiles for Run No. 19.

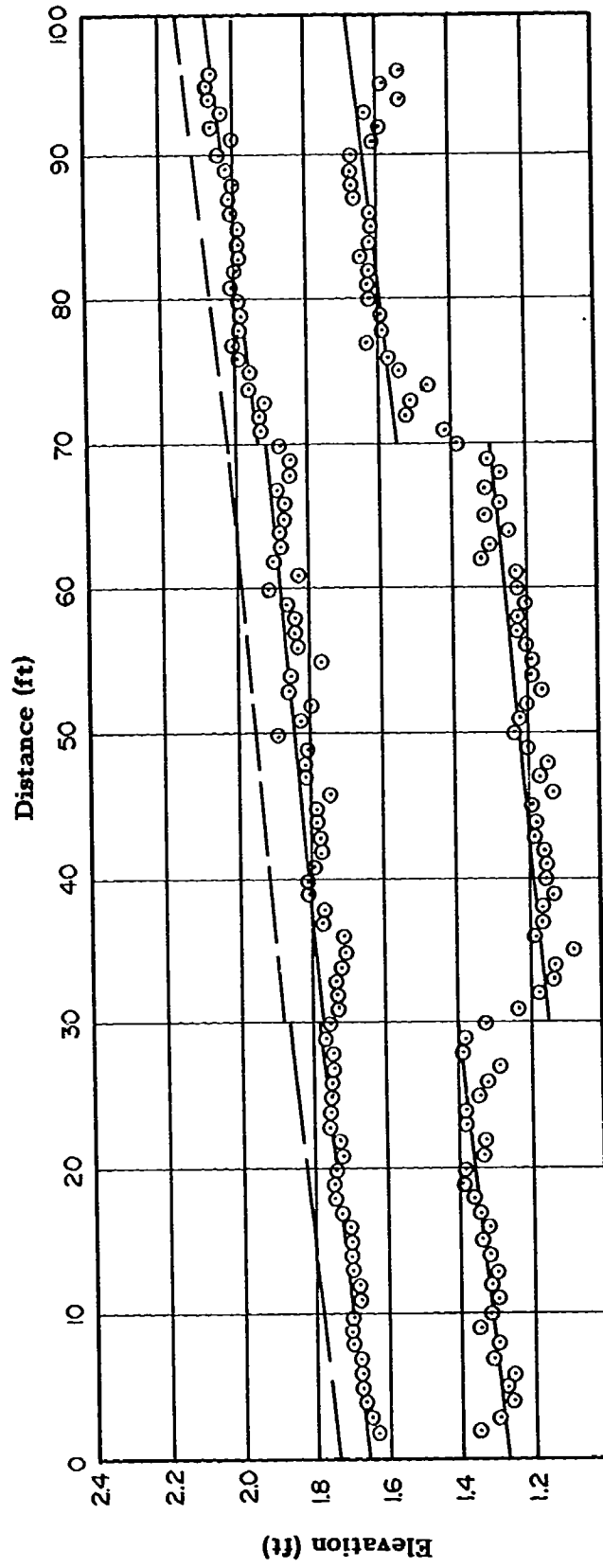


Figure 37. Profiles for Run No. 20.

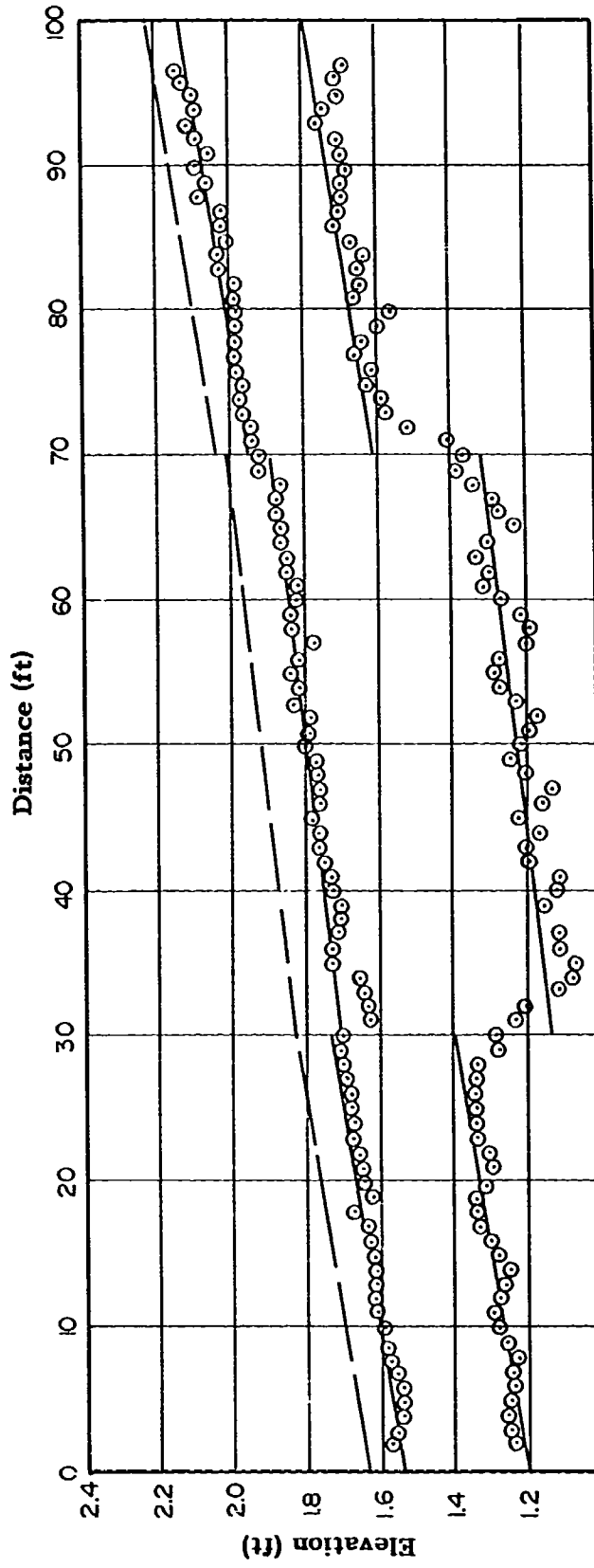


Figure 38. Profiles for Run No. 21.

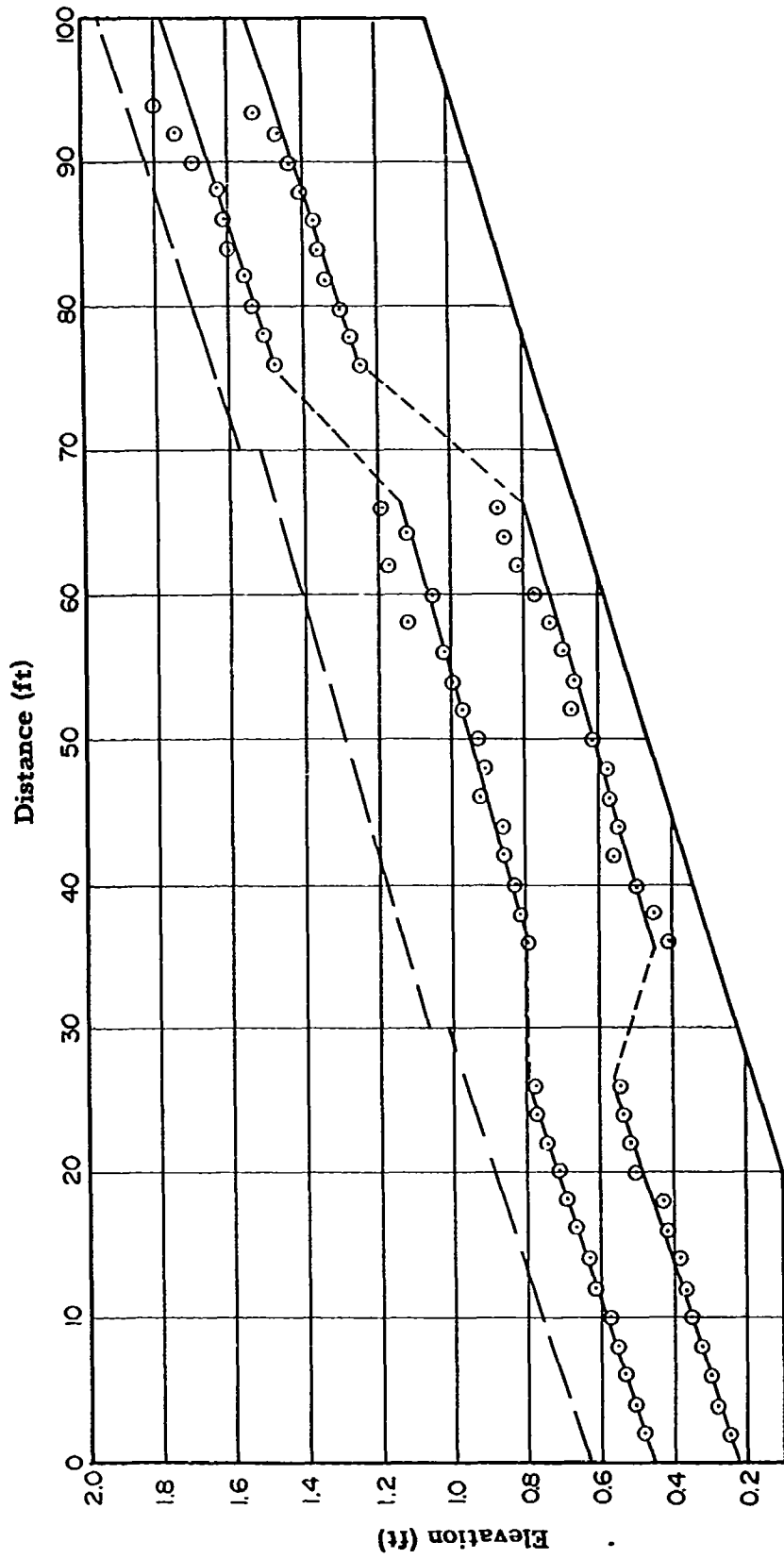


Figure 39. Profiles for Run No. 22.

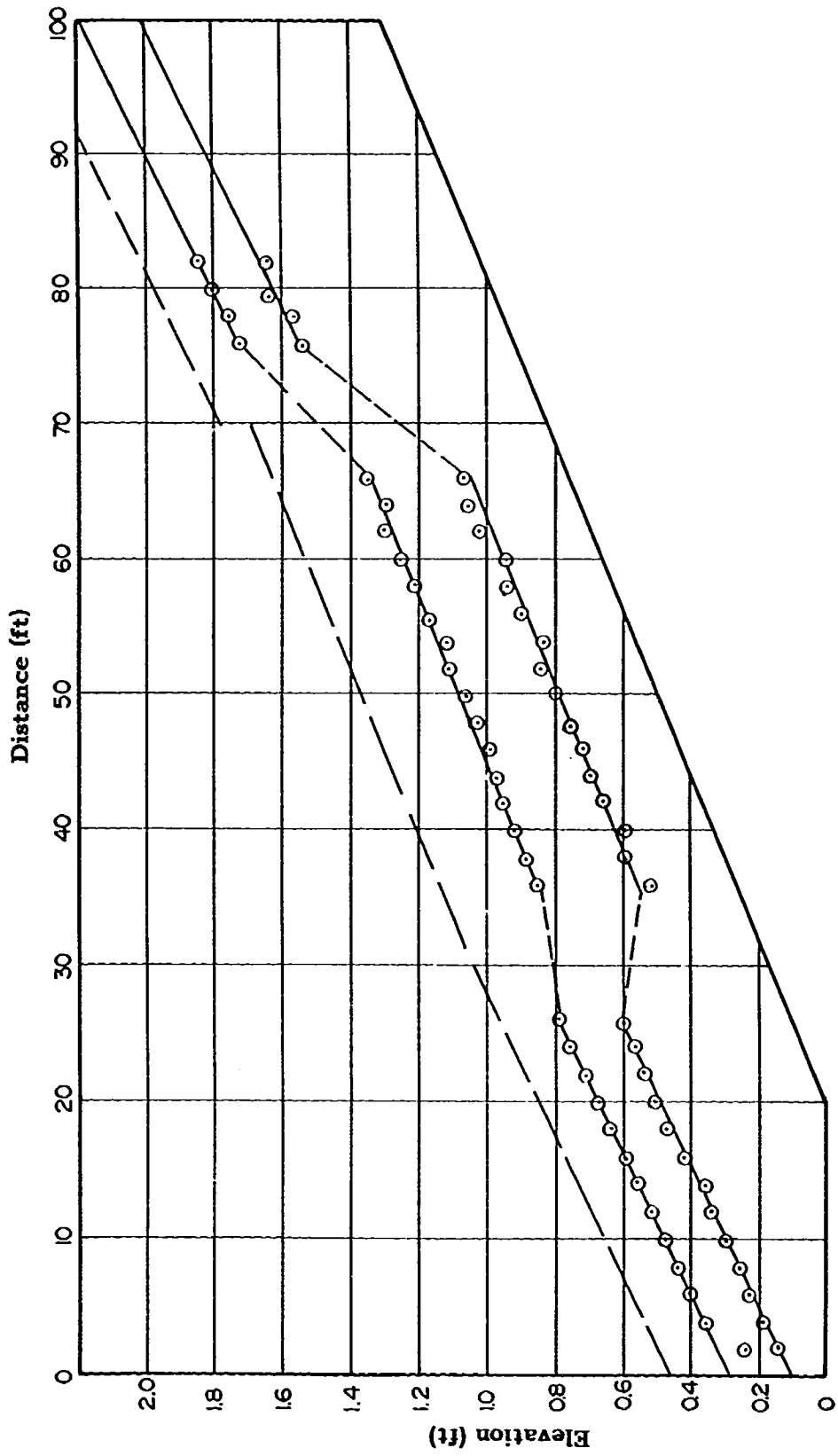


Figure 40. Profiles for Run No. 23.

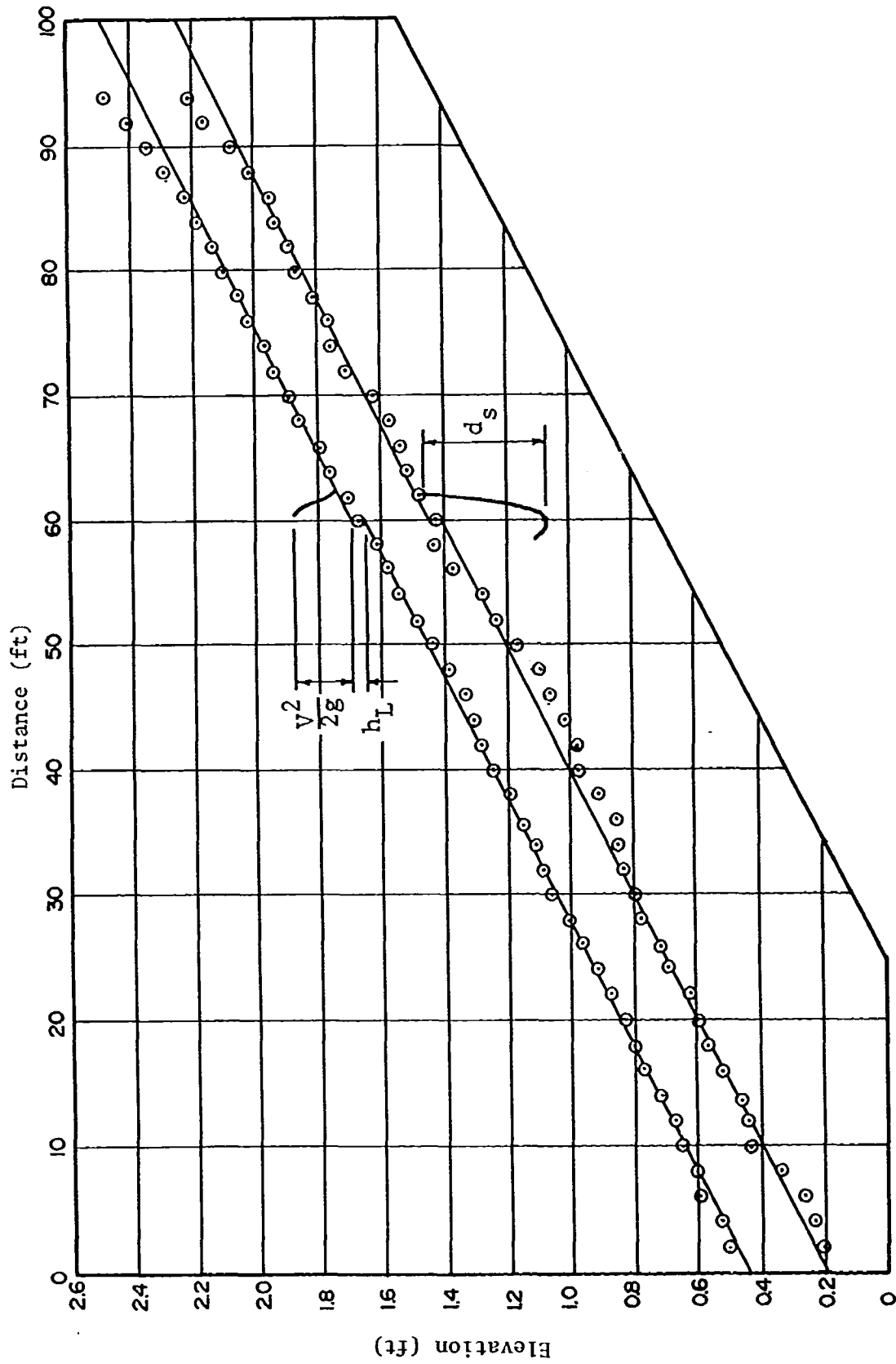


Figure 41. Backwater Run No. 24.



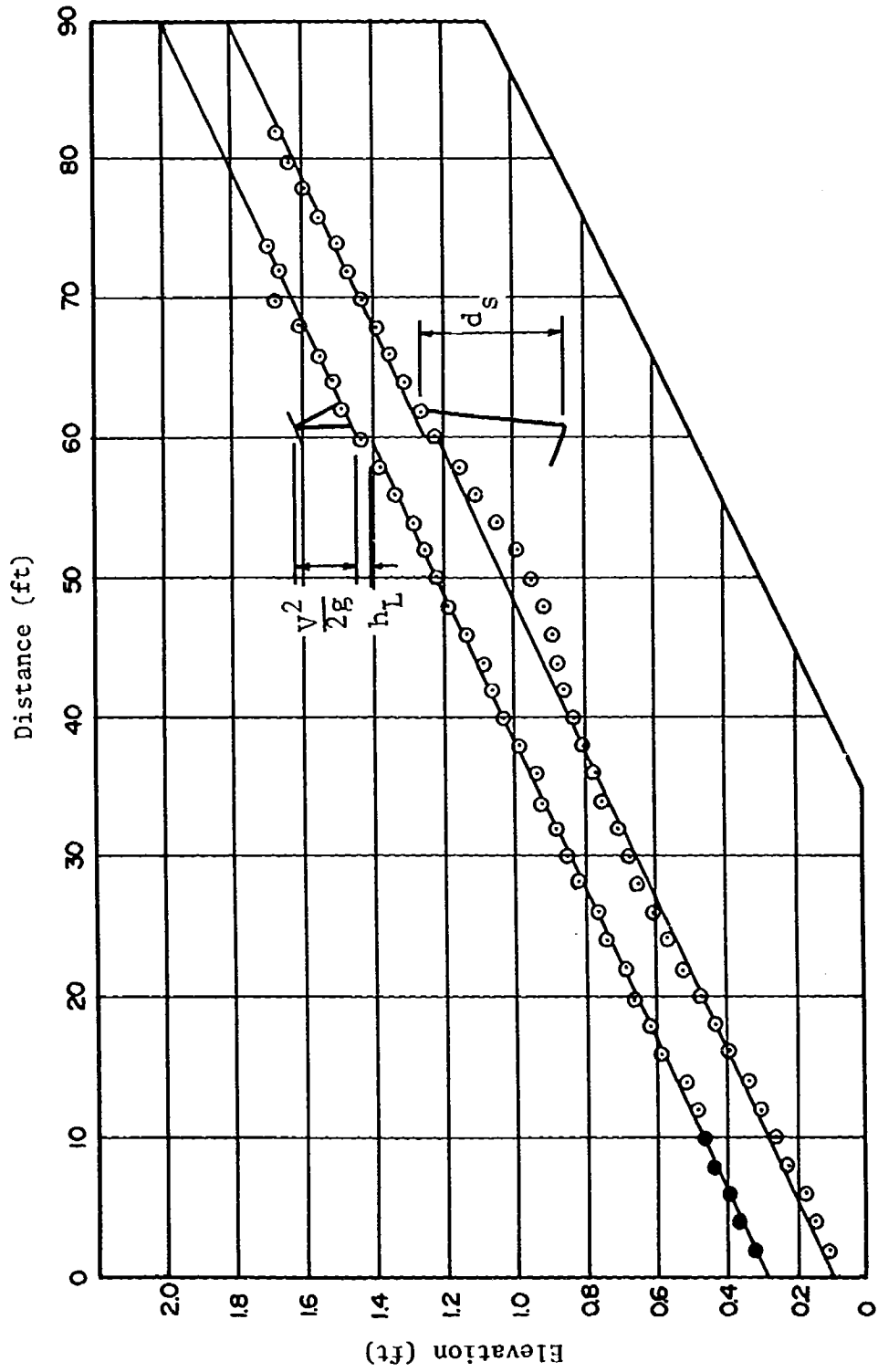


Figure 42. Backwater Run No. 25.

3. The losses in the transitions are so small as to be muddled by the errors of measurement; however, losses are apparent at the higher velocities and seem to be greater in the expanding transition than in the contracting transition -- as would be expected.
4. In the case of the abutment, the backwater is very small and only a fraction of the approach velocity head.

#### Long-Contraction Depths

The measurements of scour in the long contraction pertinent to the depth ratio are summarized in Table 3 following, and the depth ratio as measured is plotted against the  $\tau_o/\tau_c$  ratio in Figure 43 together with the predicted relationship. Too much should not be made of the measurements, but it is abundantly clear (1) that the critical tractive force in the contraction must be exceeded for anything to happen, (2) that further increases in the particle shear results in scour within the contraction, with a maximum being achieved when sediment begins to be supplied by the approach flow, and (3) that as the sediment supply increases, the relative depth of flow in the contraction becomes less -- but the scour approaches a constant, not a zero value.

Within the experimental error, the depth ratio measurements agree with the analysis. However, the agreement is not so good that it would be possible to say that the Manning equation and the Laursen sediment-transport relations

TABLE 3

## Flow Depth Measurements in the Long Contraction

<u>Gravel</u>							
Run	$\frac{Q}{(cfs)}$	$\frac{y_2}{(ft)}$	$\frac{y_1}{(ft)}$	$\frac{y_2}{y_1}$	$\frac{\tau_0'}{\tau_c}$	$F_1$	$\frac{Q_s}{(lbs/min)}$
1	2.32	0.601	---	"1"	0.23	0.29	0
2A	2.10	0.513	0.340	1.51	0.72	0.62	0
2B	2.10	0.513	0.288	1.78	1.07	0.80	0
3	2.12	0.497	0.300	1.66	0.99	0.76	0
4	2.15	0.491	0.298	1.65	1.05	0.78	1.5
5	2.23	0.474	0.292	1.62	1.17	0.83	2.5
6	2.37	0.482	0.295	1.63	1.29	0.87	6
7	2.51	0.483	0.297	1.63	1.42	0.91	7
8	2.77	0.512	0.312	1.64	1.54	0.93	15
9	3.09	0.483	0.341	1.42	1.56	0.91	40
10	2.84	0.481	0.298	1.61	1.82	1.03	40
11	2.73	0.408	0.270	1.51	2.09	1.14	50
12	2.87	0.373	0.275	1.36	2.50	1.17	90
13	3.19	0.462	0.290	1.59	2.43	1.20	90

<u>Sand</u>							
Run	$\frac{Q}{(cfs)}$	$\frac{y_2}{(ft)}$	$\frac{y_1}{(ft)}$	$\frac{y_2}{y_1}$	$\frac{\tau_0'}{\tau_c}$	$F_1$	$\frac{Q_s}{(lbs/min)}$
14	0.64	0.370	---	"1"	0.14	0.15	0
15A	0.98	0.430	0.397	1.08	0.29	0.23	0
15B	0.98	0.430	0.326	1.32	0.45	0.31	0
16	1.81	0.589	0.342	1.72	1.38	0.53	1.5
17	1.45	0.541	0.294	1.84	1.25	0.28	3
18	1.69	0.505	0.336	1.50	1.62	0.57	5
19	2.33	0.636	0.382	1.66	1.77	0.58	15
20	2.55	0.620	0.389	1.59	2.03	0.62	30
21	2.55	0.585	0.346	1.69	2.67	0.74	60
22	2.36	0.330	0.240	1.38	5.36	1.18	120
23	1.81	0.279	0.180	1.55	6.16	1.39	165

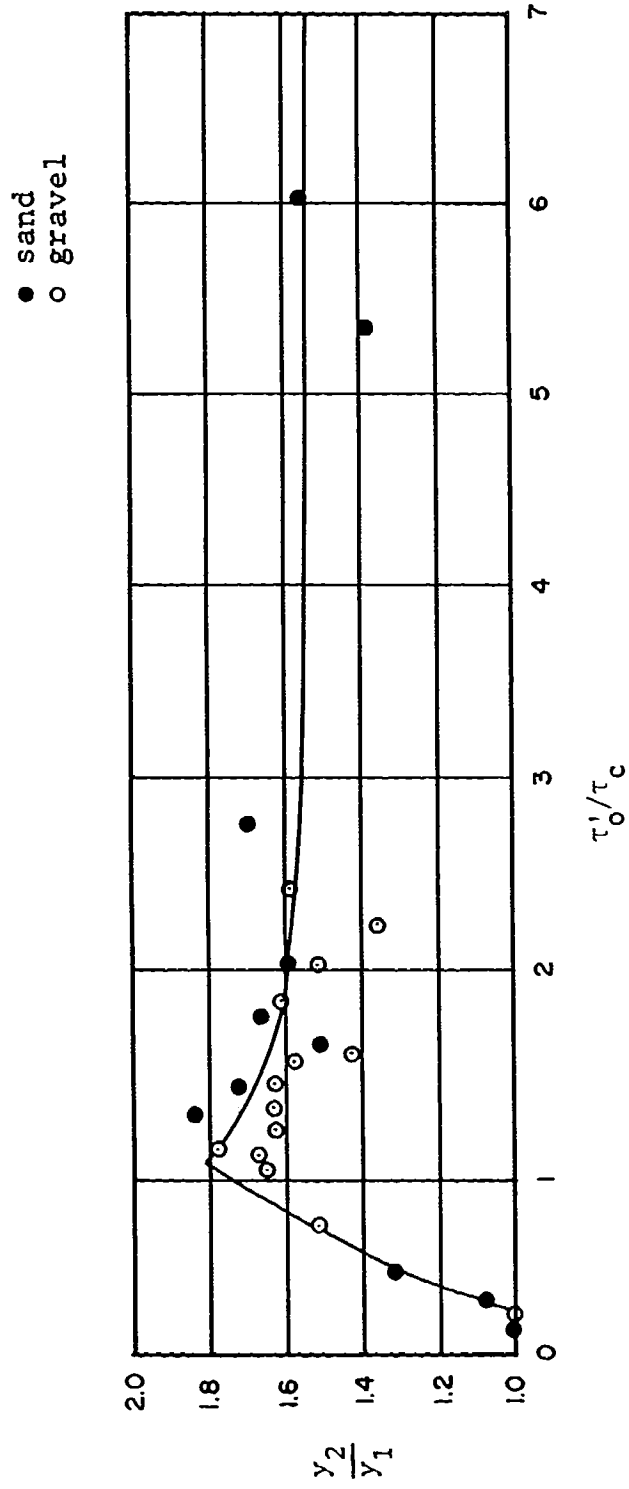


Figure 43. Long-Contraction Scour.

are the "best" available; other equations, like the Chezy or DuBoys, would give equally good agreement with the measurements. Many things contributed to the experimental difficulties, but mostly the equipment and measuring instrumentation. This is somewhat frustrating because one always likes to obtain perfect, reproducible, precise, unambiguous measurements, but in the end it does not matter so much when put in the context of applying the conclusions of the investigation to real life problems.

At the lowest discharge when movement just started in the contraction, the slope of the flume and state of the bed was not such as to establish the flow everywhere as it presumably should have been. The gravel and the sand were not single-size sediment; therefore, there was some question about whether the median-size particles were moving or not. In addition, of course, there is a question about whether the particle-shear/critical-tractive-force ratio is "correctly" evaluated. The agreement between measurement and theoretical analysis is sufficient, and definitely establishes that a finite boundary shear is required for the first particles to move. At lesser discharges, no movement could be observed.

At higher discharges, but not high enough to cause movement in the approach (wide) reach, there was definite movement in the contracted (narrow) reach and, therefore, a supply of sediment to the next wide reach. The contraction scoured until there was no further movement, and the wide,

downstream reach filled with the material being scoured out. Run 2A compares conditions in the approach and in the contraction; Run 2B compares conditions in the next wide reach and in the contraction. Run 2 seems to have worked quite well in describing conditions just before movement started in the approach (Run 2A), and as they would have been if the flow had been set so movement just started in the approach (Run 2B). Perhaps the run was not continued long enough (only forever would be theoretically long enough, since it is an asymptotic process), certainly there is error in the measurements, and again there is the question of the evaluation of the shear ratio. Nevertheless, the measurements agree very well with the analysis. Run 15 was a similar attempt to set up these conditions with the sand rather than the gravel as the sediment; it was not as successful. However, if the depth in the downstream, wide section was taken as the depth of flow at the beginning of that reach instead of the average in the reach, the shear ratio,  $\tau_{01}'/\tau_c$ , would become 1.08. Thus, it would seem that the measurements are meaningful and can be interpreted as describing the scour process in clear-water flow.

At still higher discharges, sediment moved in the approach, supplying sediment to the contraction. To the extent scour occurred in the contraction, the sediment supply to the next wide reach was greater than the amount being moved in the wide approach reach. For any given discharge and sediment load

(concentration and composition), and setting of the tailgate, there would be some certain bed configuration throughout the flume, a certain water surface profile -- and, therefore, depths of flow, velocities of flow, slopes, boundary shears and particle shears. Flow conditions should be the same in the two wide reaches except that they are offset vertically due to different conditions in the overall contraction (including the transitions).

For the clear-water (or zero-supply) case, the bed of the approach reach should not change during a run, and the water-surface profile should not change very much in the approach because the scour in the contraction and fill in the next wide section should tend to compensate. For the sediment-transporting (or sediment-supply) case, the entire bed undergoes a change as supply and capacity must balance for every section in the flume. The clear-water case takes time because it is an asymptotic process. Low concentrations in the sediment-transporting case take time because the volume rate of movement tends to be small in comparison to the volume involved in the change in the bed configuration. Moreover, all reaches of the flume must attain equilibrium -- and all reaches depend on all other reaches. The bed can react quicker if the concentration is high. However, the bed will also react quickly to any change in the rate of sediment supply to the flume.

In Runs 9, 12, and 22, the depth ratio is below the scatter band (i.e., the scour is less) which clusters about the analytical curve. No difference in behavior was noted that would explain why the scour was less in these runs, but it is quite possible that they were not run long enough to attain equilibrium. The water-surface and bed profiles could be drawn, or the measurements could be selectively interpreted to move these points in Figure 43 up to the scatter band -- they are not that different from the other runs. What is important is that the scatter band shows a decrease in the depth ratio of about 20% with an increase in the shear ratio and the rate of transport, and that most of that decrease occurs for an increase of the shear ratio from unity to two. That is to say that as the discharge and velocity and Froude number increase (everything else that can remain constant, remaining constant), the scour decreases -- in the sediment-transporting case. This is in sharp contrast to the clear-water case where the scour increases with an increase in discharge, velocity, and Froude number.

#### Long-Contraction Slopes

The scour (or depth of flow in the contraction) was the main focus of this investigation. The measurements, however, also provided information on the slopes in the normal, wide reaches and the narrow, contracted reaches as shown in Table 4 following. In all runs the slope in the contraction was less



TABLE 4

Slope Measurements in the Long Contraction

Gravel									
Run	$S_1$	$S_2$	$\frac{S_1}{S_2}$	$n_1$	$n_2$	$\frac{n_1}{n_2}$	$\frac{K_2}{K_1}$	$\frac{\tau_0}{\tau_C}$	
4	0.0088	0.0040	2.20	0.0230	0.0148	1.554	0.704	1.05	
5	0.0073	0.0036	2.03	0.0196	0.0125	1.568	0.732	1.17	
6	0.0088	0.0039	2.26	0.0205	0.0125	1.640	0.728	1.29	
7	0.0105	0.0041	2.56	0.0214	0.0122	1.754	0.728	1.42	
8	0.0117	0.0060	1.95	0.0223	0.0137	1.636	0.730	1.54	
9	0.0152	0.0091	1.67	0.0259	0.0148	1.750	0.747	1.56	
10	0.0157	0.0099	1.59	0.0232	0.0165	1.399	0.730	1.82	
11	0.0167	0.0120	1.39	0.0214	0.0151	1.417	0.764	2.09	
12	0.0255	0.0185	1.38	0.0258	0.0156	1.654	0.789	2.50	
13	0.0217	0.0180	1.21	0.0233	0.0188	1.234	0.760	2.43	
Sand									
Run	$S_1$	$S_2$	$\frac{S_1}{S_2}$	$n_1$	$n_2$	$\frac{n_1}{n_2}$	$\frac{K_2}{K_1}$	$\frac{\tau_0}{\tau_C}$	
16	0.0020	0.0003	6.67	0.016	0.005	3.200	0.688	1.38	
17	0.0025	0.0005	5.00	0.018	0.009	2.000	0.695	1.25	
18	0.0030	0.0005	6.00	0.018	0.007	2.571	0.732	1.62	
19	0.0028	0.0026	1.08	0.018	0.015	1.200	0.679	1.77	
20	0.0043	0.0033	1.30	0.020	0.015	1.333	0.689	2.03	
21	0.0063	0.0046	1.37	0.019	0.017	1.118	0.685	3.00	
22	0.0132	0.0118	1.12	0.018	0.013	1.385	0.006	5.35	
23	0.0195	0.0164	1.19	0.018	0.015	1.200	0.016	6.16	

than the slope in the wide reaches. This was largely a matter of the ratio of the Manning  $n$  values. For the gravel runs, the  $n$  values in the contraction were only 65% of the  $n$  value in the wide reach. The width/depth ratio in the flume was less than what one would expect in rivers, and the sides were, therefore, more influential. The sides in the contraction were much smoother (sheet metal) than the sides of the flume (old steel with several coats of paint over the years). The  $K$  ratio was also important in these flume experiments although the ratio did not vary much. The hydraulic radius is a fraction of the depth of flow, that fraction being the  $K$  value, and  $K$  is smaller in the contraction than in the approach. With the greater width/depth ratios expected generally in rivers, both  $K$  values would be closer to unity and the ratio of the  $K$  values even closer to unity. Thus, the absolute values of the slope ratio from the experiment should not be applied to the field; only the qualitative findings are meaningful. The slope ratio can be predicted and also the decreases in the slope ratio as the shear ratio increases. However, it is not simply a matter of the ratio of the particle shear to the critical tractive force of the approach that causes the decrease in the slope ratio, but the  $C$  ratio in the contraction and the approach ( $C$  being a simple function of the particle-shear/critical-tractive-force ratio).

With some scatter, the  $n$  values were relatively constant for the gravel runs and the slope values increase, as they should, with the velocity of flow. For the sand runs, the  $n$  values were smaller, and for the contracted reach the three lowest velocities of sediment transporting flow, the  $n$  values were unbelievably small -- resulting in slope ratios unbelievably high. The slopes in the contraction for these runs could be redrawn to obtain "better" results, but to get good results would be difficult. What is more important is that the tendencies are the same for sand as for gravel, and what would be expected from analysis. The principal difficulty in applying the slope behavior tendencies to the field is the independent prediction of the  $n$  values. Indeed, it should be noted that the  $n$  values recorded here were obtained by using the measured slope, depth and discharge values.

#### Backwater

The two other experiments using the 100-foot flume were not long-contraction scour behavior studies, but backwater at bridge opening studies. The long-contraction inserts were removed and a 45° wing-wall abutment was placed in the flume. It projected six inches into the flume and obstructed 17% of the 3-foot wide flume. A run with gravel and a run with sand were made; both were supercritical flow. As can be seen in Figures 41 and 42, the backwater was very slight; in fact, parallel straight lines through the water-surface and bed measurements (showing no backwater) would not be unreasonable.

The lines that were drawn show a backwater of  $0.17 V_A^2/2g$  (where  $V_A$  is the velocity of approach, not the nominal velocity in the bridge opening). This agrees perfectly (but honestly and accidentally) with the proposition that if a scour hole forms with the obstructed flow contained within the scour hole as a spiral roller, that the backwater will be due to the energy in the obstructed flow being lost.

In a real river it is possible that the net backwater could be even less. If the obstructed flow from the sides (or overbank) cannot spread out after going through the bridge opening, it will form a long-contraction scour condition downstream of the bridge. The slope in this self-formed long contraction can have a lesser slope than the normal river, and the resulting net effect on the backwater above the bridge should be still less -- it is even conceivable that it could be negative. Certainly, measurements of backwater at bridges over streams with erodible beds are needed, especially in the Southwest where approach velocity heads can easily be four feet and nominal velocity heads in the bridge opening considerably greater than four feet.

## THE MEASUREMENTS OF ABUTMENT SCOUR

### General Findings

The measurements of scour at the abutment agreed very well with the predicted relationships described and explained previously, and with the long-contraction scour measurements.

The scour at the abutment was greater, as expected, than the long-contraction scour, but had the same dependence on the particle-shear/critical-tractive-force ratio ( $\tau_1'/\tau_c$ ); increasing from zero scour to a maximum for clear-water flow, and then decreasing slightly as sediment began to be transported, leveling off at a finite predictable value.

The pier that was installed also scoured, but the scour depths were small because the width of the pier was small. As a result, the measurement error almost totally obfuscated the variation in scour, and it can only be stated that qualitatively the pier had the same dependence on  $\tau_1'/\tau_c$  as the abutment. The abutment, of course, can also be interpreted as a very wide pier.

No difference in flow or scour behavior was noted as the flow became critical and then supercritical. It was difficult to add the sediment at a constant rate; the runs had to be short, the velocity was high, changes in the bed took place rapidly, the stagnation ride-up was large, but these were only matters of degree -- not differences in behavior. It seemed that the width/depth ratio of the scour hole decreased, but not enough to be measurable. About a quarter of an inch of slumping into the bottom of the scour hole was observed when a run was stopped. A steeper scour hole (the boundary shear of the horseshoe vortex holding the sand or gravel at a slope steeper than the angle of repose) would result in a deeper scour hole because the sediment supply to the scour hole would

be reduced. The obstruction did not cause a hydraulic jump to form or the flow to become unstable. The flow approaching the obstruction (the abutment) dove into the scour hole (as usual) and exited in the tail of the scour hole, mixing with the unobstructed flow. A dune formed in the lee of the scour hole as it does in subcritical flow. Supercritical waves did not form.

#### Abutment Scour Depths

The measurements of scour and other variables are summarized in Tables 5 and 6 together with various parameters calculated based on those measurements. A finite discharge was necessary to observe the first particles moving at the upstream corner of the abutment. Thereafter, the depth of scour increased with the discharge until movement began generally in the flume supplying sediment to the scour hole. The depth of flow could not be held to the same value in the various runs with the consequence that the length of abutment/depth of flow ratio varied somewhat. In order to remove this third factor from consideration, the measured ratio of depth of scour to depth of flow was divided by the "theoretical" or predicted depth of scour for a high rate of sediment transport. Because the width/depth ratio of the scour hole was found to be 2.0 rather than 2.75, this correction was made in the predicting equations (Figs. 44 and 45). Figure 46 is a plot of the data so interpreted; the measurements scattering about the predicted relationships for clear-water and sediment-transporting flow.

TABLE 5  
Measurements of Abutment (Pier) Scour

Run	<u>Gravel</u>										
	$Q$ (cfs)	$d_s$ (ft)	$y_o$ (ft)	$\frac{d_s}{y_o}$	$\frac{x}{y_o}$	$\frac{\tau_o'}{\tau_c}$	$F_o$	$\frac{d_{sLim}}{y_o}$	$\frac{d_{smeas}}{d_{sLim}}$	$\frac{Q_s}{(lbs/min)}$	
1	1.31	0	0.325	0	1.60	0.18	0.31	2.26	0	0	
2	1.74	0.402	0.306	1.31	1.70	0.35	0.45	2.33	0.59	0	
3	1.80	0.744	0.287	2.59	1.81	0.44	0.51	2.40	0.75	0	
4	2.48	0.767	0.301	2.55	1.73	0.76	0.66	2.35	1.09	0	
5	2.42	0.731	0.252	2.90	2.07	1.09	0.71	2.57	1.13	0	
6	2.92	0.774	0.326	2.37	1.60	0.87	0.69	2.26	1.05	0	
7	3.25	0.840	0.329	2.55	1.58	1.05	0.75	2.25	1.13	1	
8	3.26	0.852	0.289	2.94	1.80	1.44	0.93	2.39	1.23	4	
9	3.48	0.728	0.317	2.29	1.64	1.32	0.85	2.23	1.03	17	
10	3.83	0.688	0.362	1.90	1.44	1.18	0.78	2.14	0.89	31	
11	3.94	0.707	0.313	2.26	1.66	1.74	0.99	2.29	0.99	60	
12	3.98	0.636	0.280	2.27	1.86	2.31	1.18	2.45	0.93	120	
13	4.27	0.701	0.315	2.26	1.65	2.02	1.13	2.24	1.01	114	

TABLE 6

Measurements of Abutment (Pier) Scour

Sand											
Run	$Q$ (cfs)	$d_s$ (ft)	$Y_o$ (ft)	$\frac{d_s}{Y_o}$	$\frac{k}{Y_o}$	$\frac{v_o'}{v_c}$	$F_o$	$\frac{d_{s,lim}}{Y_o}$	$\frac{d_{s,meas}}{d_{s,lim}}$	$\frac{Q_s}{(lbs/min)}$	
14	0.55	0.0	0.262	0	1.99	0.13	0.18	2.52	0	0	
15	1.06	0.133	0.334	0.398	1.56	0.28	0.24	2.24	0.18	0	
16	1.37	0.358	0.315	1.14	1.65	0.54	0.34	2.28	0.50	0	
17	1.49	0.546	0.298	1.83	1.74	0.73	0.40	2.36	0.78	0	
18	1.67	0.585	0.282	2.07	1.85	1.03	0.48	2.43	0.85	0	
19	1.77	0.6706	0.269	2.25	1.94	1.30	0.56	2.48	0.91	2	
20	1.82	0.603	0.42	2.49	2.15	1.64	0.67	2.61	0.95	6	
21	1.95	0.637	0.243	2.62	2.14	1.99	0.72	2.60	1.01	30	
22	2.23	0.563	0.251	2.24	2.08	2.42	0.78	2.57	0.87	60	
23	3.40	0.764	0.273	2.80	1.91	4.62	1.05	2.47	1.13	120	
24	2.99	0.558	0.254	2.19	2.05	4.21	1.03	2.55	0.85	142	
25	3.87	0.814	0.274	2.97	1.90	5.92	1.41	2.46	1.21	180	

Sand by Pacheco

Run	$Q$ (cfs)	$d_s$ (ft)	$Y_o$ (ft)	$\frac{d_s}{Y_o}$	$\frac{k}{Y_o}$	$\frac{v_o'}{v_c}$	$F_o$	$\frac{d_{s,lim}}{Y_o}$	$\frac{d_{s,meas}}{d_{s,lim}}$	$\frac{Q_s}{(lbs/min)}$
26	2.23	0.668	0.246	2.72	2.12	2.53	0.80	2.59	1.05	30
27	2.42	0.691	0.223	3.10	2.34	3.76	1.01	2.72	1.14	60
28	2.45	0.628	0.231	2.72	2.26	3.52	0.97	2.68	1.01	90



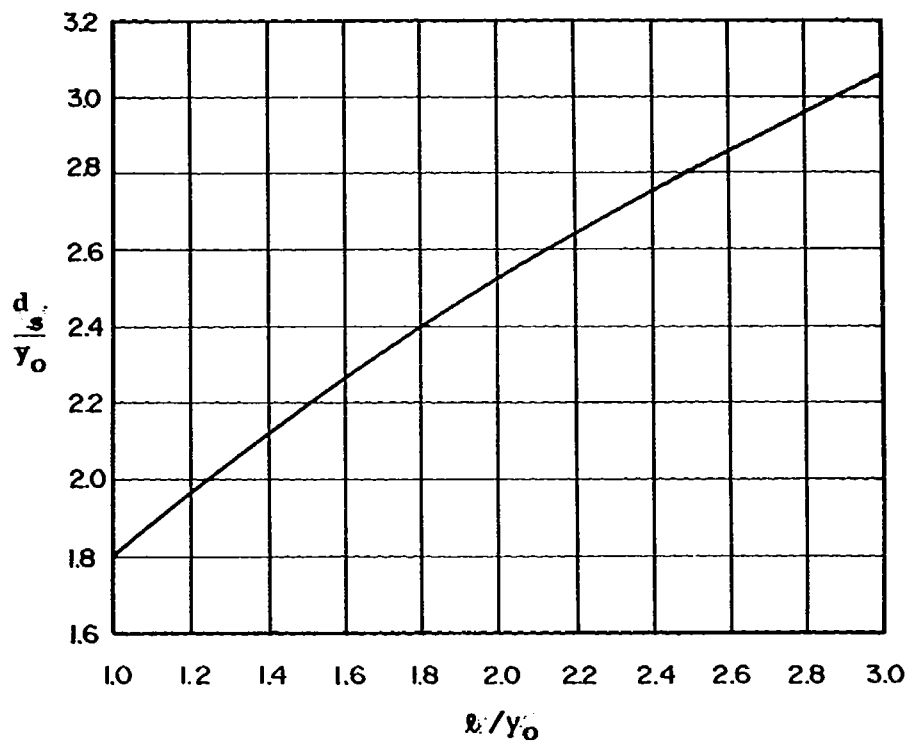


Figure 44. Revised Scour Relationship for Sediment-Transporting Flow.

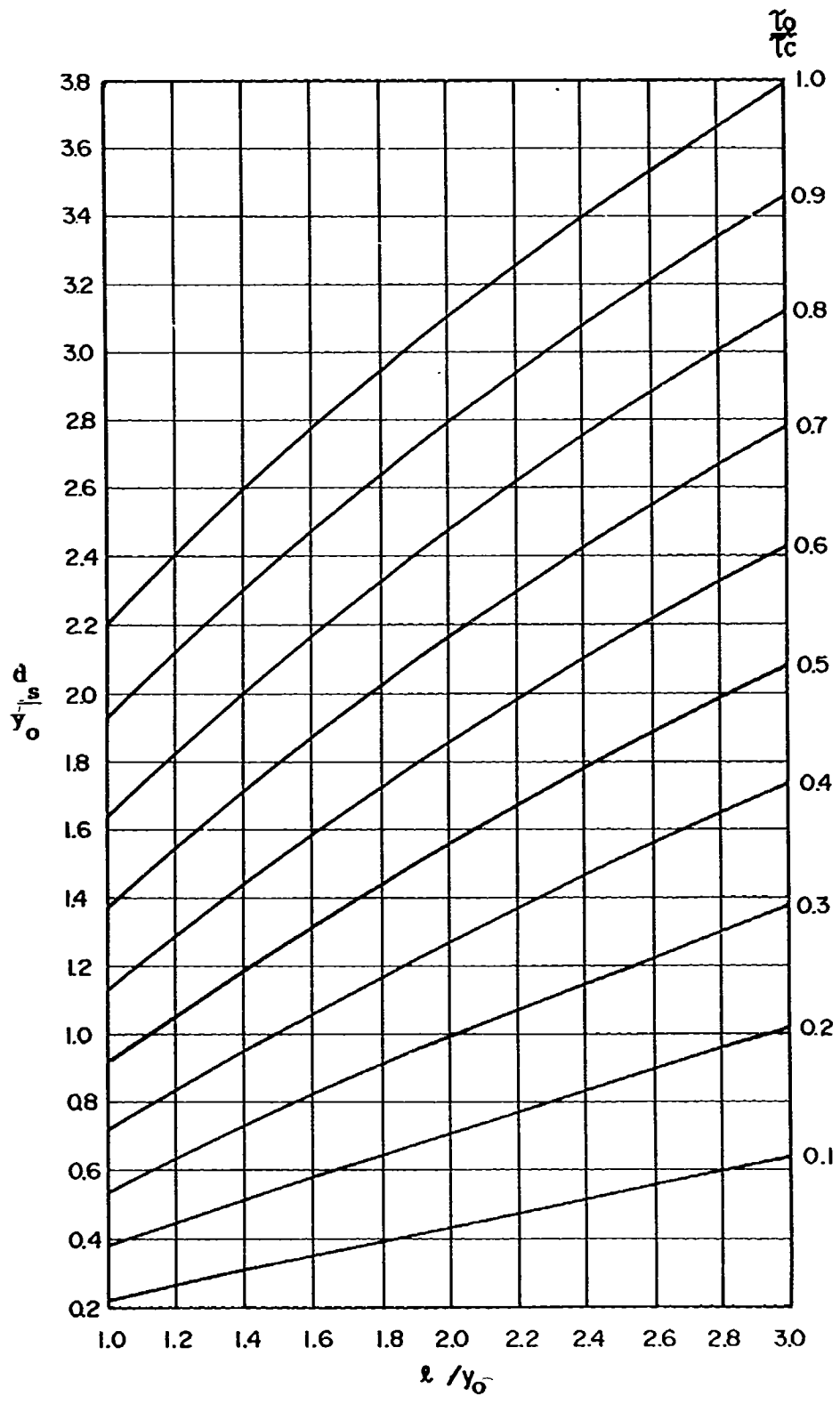


Figure 45. Revised Scour Relationship for Clear-Water Flow.

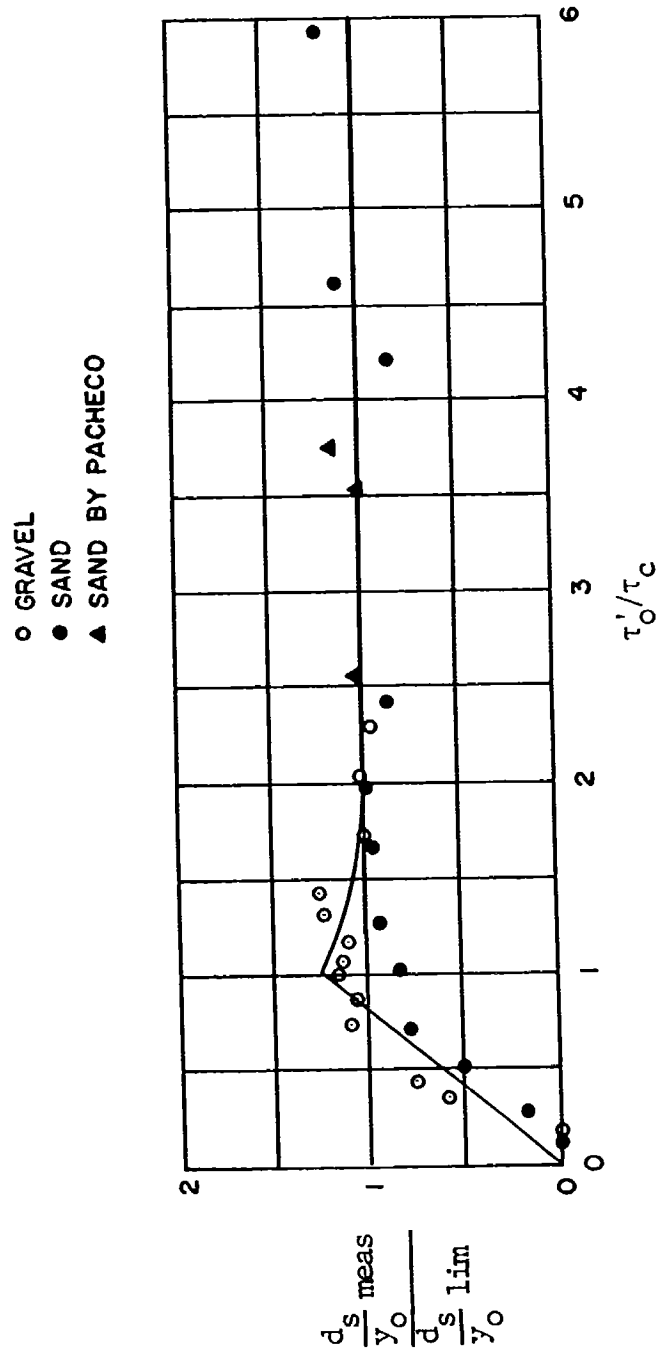


Figure 46. Relative Pier Abutment Scour.

The scatter is greater than desired, but not exceptionally so. The data is sufficient to indicate (1) that the "velocity" is important only in the clear-water scour behavior, (2) that the scour drops off slightly from the maximum as the particle-shear/critical-tractive-force ratio increased from unity to two, and (3) that for the conditions of design (the river in flood) the scour depth is a function of geometry alone -- not the velocity or the sediment size, or the Froude number.

The predicted zero depth of scour occurs when the particle shear is zero. This is because the three-dimensional diving pattern of flow is presumed in the analysis and because the width of the fictitious long-contraction goes to zero. In reality, as the depth of scour becomes very small (or zero), the flow pattern approaches the two-dimensional potential flow pattern at a contraction -- as should be expected for a rigid bed boundary situation. This discrepancy between prediction and reality has little practical significance. In using the clear-water solution for sizing riprap, placing the riprap at bed elevation results in very large stone being required. In practice, riprap should be placed at the lowest elevation possible.

The need for modification of the predicting equation to account for the steeper angle of repose opens up another aspect of scour at bridge piers and abutments. The effect is not large, and the scour hole width depth ratio is not simply the

angle of repose because the bottom of the scour is a rounded truncation of the inverted cone which is the scour hole.

### CONCLUSIONS

Despite the difficulties encountered in this experimental laboratory investigation, and the lack of precision in the data resulting therefrom, the effect of velocity on scour even into the supercritical range of flow has been found to be as described in previously expounded analyses of scour in a long contraction and scour around piers and abutments.

A distinct difference exists between clear-water scour and scour by sediment-transporting flow. In the case of clear-water scour, the limit to the extent of scour is reached when the particle boundary shear is equal to the critical tractive force of the sediment particles making up the erodible boundary. The depth of scour is then a function of the ratio of the particle shear to the critical tractive force; the velocity is an important variable in determining the particle shear, and the sediment size is an important variable in determining the critical tractive force. There are several other factors involved directly and indirectly in this ratio, and there could be various ways to approximately evaluate this ratio; however, it appears that the evaluation of  $\tau_{01}'/\tau_c$  which has been used herein (and previously) is adequate.

In the case of scour by sediment-transporting flow, the limit is reached when the supply of sediment to the scour hole is equal to the capacity of the flow (in and out of the scour hole) to remove sediment from the scour hole. The dependence of the scour depth on the ratio of the particle shear to the critical tractive force is then small and mostly in the change of the ratio from unity to a value of about two. Interestingly, the decrease in scour depth over this increase in the  $\tau_{01}'/\tau_c$  ratio has been predicted and is a consequence of the critical tractive force term in the sediment-transport equation used in the analysis.

The behavior of the scour for both types of geometry and both kinds of scour were entirely predicted by the analyses which include the geometry of the situations as well as the velocity and sediment size effects -- or better, the  $\tau_{01}'/\tau_c$  effect. The predicting equation was modified to account for the steeper angle of repose of the sediments used in the investigation compared to the sediments used in the old Iowa experiments.

No untoward behavior was observed as the flow became (energy) critical and then supercritical. In the long contraction, antidunes formed, and in both flumes, the high velocities and high rates of sediment transport made measurements difficult. These effects, however, were expected and represented changes of degree not of fundamental behavior.

At the high Froude numbers the flow was not unstable except insofar as the train of antidunes shifted from side to side. This, however, is something that many researchers have observed and was not surprising -- and probably not a function of the scour phenomena being investigated here. It is not at all clear whether instability might result from Froude numbers greater than two when roll waves occur or from more radical geometries. The equipment could not be used for such an extension of the investigation.

The slope in the long contraction was less than in the normal, wide reach upstream and downstream. The difference in slope, however, was largely a result of the lesser Manning  $n$  value in the long contraction, which makes cause and effect ambiguous. Nevertheless, the slope behavior lends credence to the proposition that the slope in the long contraction will be less than normal for the river.

The other incidental, but very important, finding was that the backwater resulting from a bridge opening contraction is very small if scour occurs at the piers and abutments. The backwater appears to be equal to a fraction of the approach velocity head; the fraction being the fraction of the flow obstructed by the piers and abutment/embankment. This behavior is in line with the description of the flow pattern of the obstructed flow diving into the scour hole, forming a horseshoe vortex in the scour hole, and blending with the unobstructed

flow as it comes out in the tails of the scour hole. The energy of the horseshoe vortex comes from the stagnation ride-up on the piers and abutments; the stagnation ride-up comes from the velocity head of the approach flow, and the horseshoe vortex energy is finally dissipated. The resulting backwater is much less than the backwater predicted on the basis of rigid bed hydraulics.

#### RECOMMENDATIONS FOR FURTHER STUDY

Although there are still aspects of the scour problem that could be studied in the laboratory, it is much more important to obtain measurements in the field. The few measurements that have been made of scour in the field are not fully satisfying. Rather than concentrating on attempting to measure the phenomenon at flood peaks, it would be perhaps much more fruitful to measure (and remeasure) what happens during moderate flows -- it certainly would be easier. Although it is merely a consequence of scour, another important field measurement that is needed is the backwater at a bridge where scour changes (alleviates) the boundary contraction. Getting good field measurements is always a difficult task, but instrumentation and procedures for obtaining these suggested measurements exist. It is also recommended that observations be made of supercritical, sediment-transporting flow in nonuniform, unstraight channels in order to better understand the behavior of this kind of streamflow. There is still a



suspicion that this kind of flow could become unstable under certain conditions and could deposit rather than scour, contributing to the avulsions that occur on alluvial fans.

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